



UNIVERSITEIT VAN AMSTERDAM



Voluntary Participation in a Defined Benefit Pension Scheme

An Option Pricing Approach

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The U.K. (April 2015): withdraw pension assets at the age of 55
Canada (May 2015): Minister of Finance: "*consider allowing additional voluntary contributions to the country's mandatory Canada Pension Plan*"

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- What is the critical funding rate for which the collective DB pension scheme collapses and what is the probability of such an event?

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- Regulation policy to adjust financial shocks in the funding rate (F):

$$E_t^{\mathbb{Q}}(F_{t+s} - \bar{F}) = \alpha^s (F_t - \bar{F}), \quad \forall s \geq 0, \quad \alpha \in (0, 1)$$

Low α : immediate recovery

High α : smoothing risks by allowing funding rate fluctuations

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 - exercise at each date until retirement (*American*)
- Main contribution of this paper is to model participation decisions as an American option to explore stability of the pension scheme

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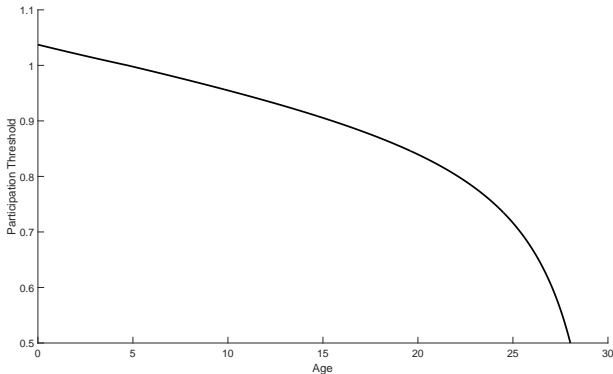
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- Elderly are more willing to stay due to the uniform contribution rate (“doorsneesystematiek”), because of the *“PAYG-element”* in it
- Including more exercise dates increases the willingness of the young to participate and, hence, stability of the collective pension scheme increases

Benchmark Parameters

Description	Symbol	Value
Entry age	t_0	0
Retirement age	t_R	40
Age of death	t_D	60
Target funding rate	\bar{F}	1
Risk smoothing	α	0.5
Interest rate (risk free)	r	0.02
Portfolio return volatility	σ	0.15
Wage	w	1
Accrual rate	ψ	70%/ t_R

European Option

Participation Tresholds



Exercising the option can be beneficial for a young agent when the funding rate is particularly low. An entry generation participates voluntarily for $F_0 \geq 103.7\%$

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- Overview of the funding rate thresholds for an entry generation:

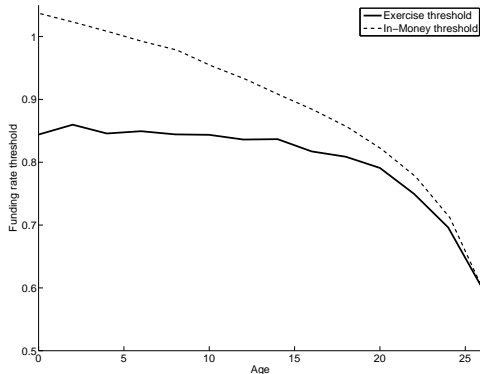
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 - European option: threshold = 103.7%
 - Bermudian option: threshold = 96.3% (shown in the paper)
 - American option: threshold = 84.4%

American Option

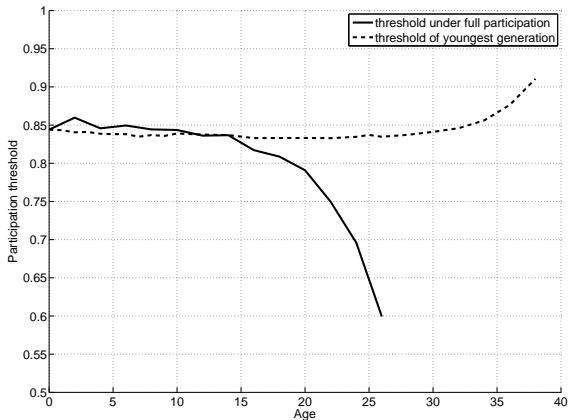
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 - European option: threshold = 103.7%
 - Bermudian option: threshold = 96.3% (shown in the paper)
 - American option: threshold = 84.4%
- Agents are more inclined to stay when there are more exercise dates (i.e. more flexibility), because quitting is possible at a later stage as well under the American option.

Participation Thresholds



Dashed line: European option (103.7% at the age of $t_0 = 0$)
Solid line: American option (84.4% at the age of $t_0 = 0$)

Equilibrium



The graphs cross at a funding rate of 83.8% and age 11.5

Three Scenarios under the American Option

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- (ii) Funding rate $83.8\% \leq F_t < 84.4\%$:
 - a small group of agents exercise the option, but most generations stay in the collective pension scheme

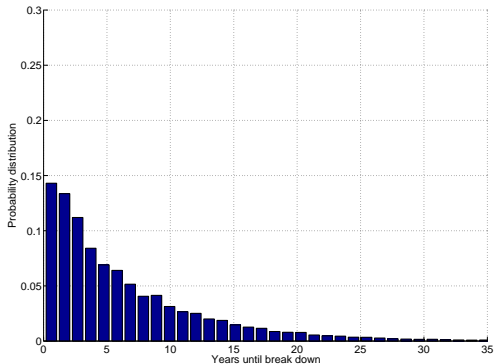
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- (i) Funding rate $F_t \geq 84.4\%$:
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- (ii) Funding rate $83.8\% \leq F_t < 84.4\%$:
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- (iii) Funding rate $F_t < 83.8\%$:
 - a large group of generations leave the collective pension scheme. As a result, the thresholds of older generations increase and, therefore, they prefer to leave the collective scheme as well. Hence, a chain reaction of cohorts exercising the option occurs and the collective system collapses

Break-Down Distribution



The probability that the pension fund survives at least 20 years (10 years) is about 5% (20%).

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Conclusion

- Participants are more inclined to stay when there are more exercise dates (i.e. more flexibility)
- Particularly young are willing to exit if the funding rate is low
- Risk smoothing and investment risk increases the survival probability of the collective DB pension scheme
- However: the collective pension scheme collapses almost surely after 20 to 40 years depending on the parameter settings
- In the absence of mandatory participation, it is only a matter of time before such a break-down occurs

Additional Slides

Related Literature

- **Benefits from collective funded pension plans:** Teulings and De Vries (2006); Ball and Mankiw (2007); Gollier (2008); Cui et al. (2011); Chen et al. (2014)
- **Conditions on voluntary participation in funded pension schemes:** Hemert (2005); Bommel (2007); Siegmann (2011); Beetsma et al. (2013); Beetsma and Romp (2013)
- **Applying option pricing theory to pensions:** Fung and Chan (1995); Blake (1998); Kocken (2006); Timmermans et al. (2011); Broeders et al. (2013)
- **American option of early retirement:** Friedman and Shen (2002); Chevalier (2006)
- **Least Squares Monte Carlo (LSMC) approach to value pension and life insurance products:** Pelsser et al. (2007); Bernard and Lemieux (2008); Cathcart and Morrison (2009); Boyer and Stentoft (2013); Chen (2015)

Tradeoff Mandatory vs. Voluntary Participation

- Arguments that advocate mandatory participation:
 - protection against complex investment decisions and myopia
 - costs reduction
 - facilitate (intergenerational) risk-sharing arrangements

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 - protection against complex investment decisions and myopia
 - costs reduction
 - facilitate (intergenerational) risk-sharing arrangements

- Arguments that advocate voluntary participation:
 - lack of trust
 - increasing life expectancy
 - freedom of choice & heterogeneous preferences
 - increasing labor mobility & self employment

Value of Participation

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- Value of participation at age $t_M =$

$$\underbrace{\exp[-r(t_R - t_M)] \Pi_{t_R}(B_{t_R})}_{\text{Discounted future retirement benefits}}$$

Discounted future retirement benefits

$$- \underbrace{E_{t_M}^Q \left[\int_{t_M}^{t_R} c_s \exp[-r(s - t_M)] ds \right]}_{\text{Discounted expected contribution payments}}$$

Discounted expected contribution payments

$$- \underbrace{\min(1, F_{t_M}) \Pi_{t_M}(B_{t_M})}_{\text{Value obtained from exiting}}$$

Value obtained from exiting

Participation Decision at Retirement

- Value of participation at the age of t_R , i.e. the retirement age:

$$\begin{aligned} \text{Participation}_{t_R} &= \underbrace{\Pi_{t_R}(B_{t_R})}_{\text{PV benefits}} - \underbrace{0}_{\text{Contributions}} - \underbrace{\min(1, F_{t_R}) \Pi_{t_R}(B_{t_R})}_{\text{Value from exiting}} \\ &= \max(0, 1 - F_{t_R}) \Pi_{t_R}(B_{t_R}) \end{aligned}$$

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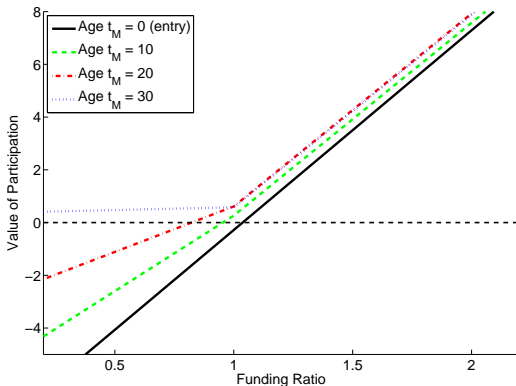
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- Overfunding: $\text{Participation}_{t_R} = 0$

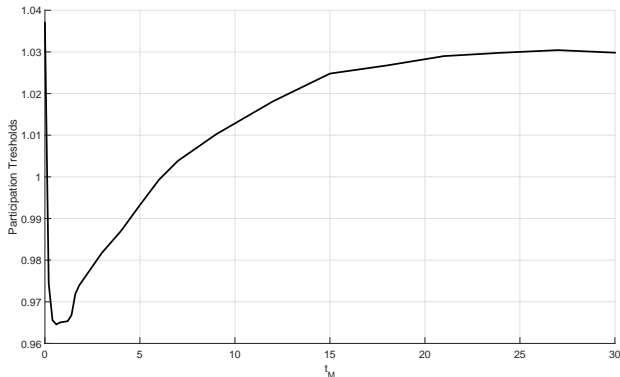
Underfunding: $\text{Participation}_{t_R} = (1 - F_{t_R}) \Pi_{t_R}(B_{t_R}) > 0$

Value of Participation at ages 0, 10, 20 and 30



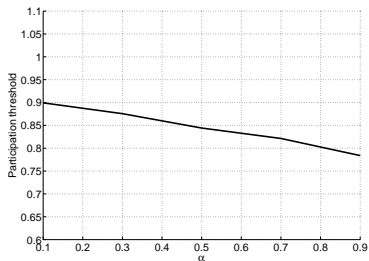
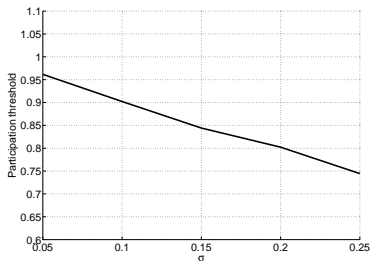
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Decision at Entry and Another Arbitrary Age (Bermudian Option)

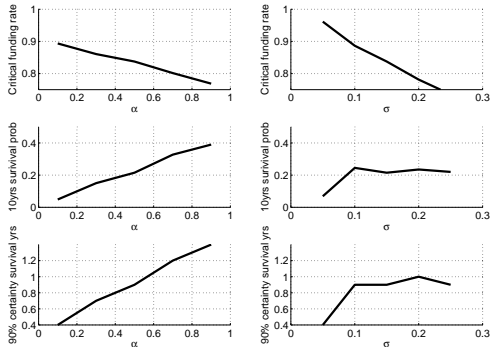


Additional exercise date most valuable at ages $t_M \in [0.5, 5.0]$

Investment Risk and Recovery Smoothing

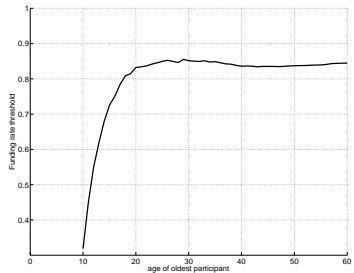
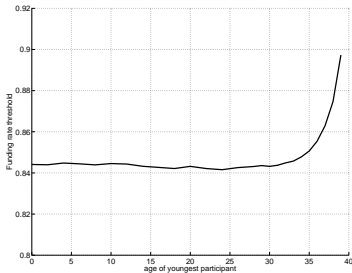


Smoothing and Investment Risk



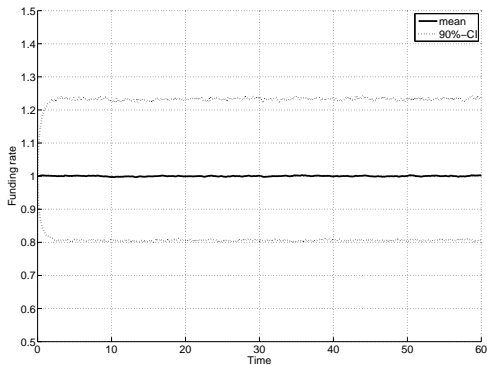
The critical funding rate decreases for a longer recovery window (α) and for higher investment risk (σ). However, these parameters also raise the funding rate volatility.

Entry Generations



A relatively old pension scheme is unattractive for entry generations, causing the thresholds to increase (**left**). Vice versa, for a relatively young pension scheme (**right**).

Funding Rate Simulations



At least 5% of the funding rate simulations are below the critical level of 84.4%.

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- 6 Repeat steps 3 to 5 until date $t_0 = 0$ is reached.
- 7 The value of participation at time t is then given by:
$$Participation_t = \frac{1}{Q} \sum_{i=1}^Q (Cont_{t,i} - Stop_{t,i})$$

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