



Network for Studies on Pensions, Aging and Retirement

# The impact of uncertainty in risk preferences and risk capacities on lifecycle investment

*Anne G. Balter  
Rob van den Goorbergh  
Nikolaus Schweizer*

DESIGN PAPER 237

NETSPAR INDUSTRY SERIES

**DESIGN PAPERS** are part of the **refereed Industry Paper Series**, which are refereed by the Netspar Editorial Board. Design Papers discuss the design of a component of a pension system or product. A Netspar Design Paper analyzes the objective of a component and the possibilities for improving its efficacy. These papers are easily accessible for industry specialists who are responsible for designing the component being discussed. Authors are allowed to give their personal opinion in a separate section. Design Papers are presented for discussion at Netspar events. Representatives of academic and private sector partners, are invited to these events. Design Papers are published at the Netspar website.

### **Colophon**

Netspar Design Paper 237, November 2023

### **Editorial Board**

Mark-Jan Boes – VU Amsterdam  
Andries de Grip (chairman) – Maastricht University  
Marcus Haveman (NN)  
Arjen Hussem – PGGM  
Kristy Jansen – University of Southern California  
Agnes Joseph – Achmea  
Serge Mans – AEGON  
Raymond Montizaan – Maastricht University  
Alwin Oerlemans – APG  
Maarten van Rooij – De Nederlandsche Bank  
Mariëtte Sanderse – PMT  
Peter Schotman – Maastricht University  
Erik Schouten – Ministry of Finance | Belastingdienst  
Frank Smudde – APG  
Jeroen Wirschell – PGGM  
Marianne Zweers – a.s.r.

### **Design**

B-more design

### **Lay-out**

Bladvulling, Tilburg

### **Editors**

Frans Kooymans, Frans Kooymans-Text and Translation and Netspar

Design Papers are publications by Netspar. No reproduction of any part of this publication may take place without permission of the authors.

# CONTENTS

<i>Summary</i>	4
<i>Samenvatting</i>	5
1. <i>Introduction</i>	6
2. <i>The setting</i>	10
3. <i>Results and discussion</i>	16
4. <i>Practical challenges</i>	30
5. <i>Conclusion</i>	32
<i>References</i>	33

## **Affiliations**

Anne G. Balter – Tilburg University

Rob van den Goorbergh – APG

Nikolaus Schweizer – Tilburg University

## Summary

We study the impact of suboptimal lifecycle investment as a result of changing risk preferences and unanticipated shocks in income. In particular, we consider the possibility that risk aversion varies with age, and we measure the welfare effect when the risk exposure decided on earlier in life was based on a wrong or outdated assessment of one's risk aversion. Moreover, we explicitly model the lifecycle and allow for wrong expectations about future income and thus about future pension contributions. We find that leverage constraints bound the losses caused by underestimation of risk aversion. A drop in pension accrual due to circumstances such as disability, self-employment, emigration, or part-time work can cause considerable losses, especially when the risk aversion level is underestimated.

## **Samenvatting**

### **De invloed van onzekerheid in risicopreferentie en risicocapaciteit op levensloopinvesteringen**

We bestuderen de invloed van suboptimale levensloopinvesteringen als gevolg van veranderende risicopreferenties en onverwachte inkomensschokken. We houden met name rekening met de mogelijkheid dat risicoaversie varieert met leeftijd en we meten het welvaartseffect wanneer de risicoblootstelling waartoe eerder werd besloten gebaseerd was op een verkeerde of achterhaalde inschatting van iemands risicoaversie. Verder modelleren we de levensloop expliciet en houden we ook rekening met verkeerde verwachtingen over toekomstig inkomen en daarmee over toekomstige pensioenpremies. Onze bevinding is dat leenrestricties de verliezen beperken die veroorzaakt zijn door onderschatting van risicoaversie. Een daling van de pensioenopbouw door bijvoorbeeld arbeidsongeschiktheid, zelfstandig ondernemerschap, emigratie of deeltijdwerk kan grote verliezen veroorzaken, zeker wanneer het niveau van risicoaversie wordt onderschat.

## 1 Introduction

Under new Dutch pension law, pension funds and insurance companies are required to elicit the risk preferences and risk capacities of individual participants and to adjust (collective) investment strategies accordingly. A considerable amount of recent research (e.g. Alserda et al. (2019), AFM (2023)) has studied how the risk preferences and risk capacities of participants can be measured. Our focus is on the next step, from (possibly noisy) preference measurements to investment strategies. Specific attention is given to the time dimension of the problem and the associated uncertainty, as risk attitudes and risk capacities may change over time. Moreover, there is a large variation in life paths, from the time when pension accrual begins to the pay-out phase. This uncertainty and the possible instability in preferences is a considerable threat to the potential benefits from early personalization of investment strategies.

With evolving risk preferences, an investment strategy that may look optimal to a young participant can turn out to look less promising at later points in time. Even if young participants could see into the future, they might not want to take advice from their older selves because of changing views on what constitutes an acceptable risk. Of course, this problem of evolving preferences does not exist in isolation. Besides a possible uncertainty in future preferences, there is considerable (economic) uncertainty over long horizons when it comes to human capital. Finally, the preferences at an older age should ideally guide the riskiness of investment towards retirement. Yet, these old-age preferences may not be known at the time when the investments are made.

The goal of this paper is to investigate the welfare effect arising from changes in both risk preferences and risk capacity (which we largely identify with human capital). We follow a model-based approach that uses different scenarios for both individual preferences and for the economy. Our sensitivity analyses are based on a simple “moment-of-truth” type model, where a participant realizes his or her true risk preferences or true risk capacity only at some intermediate age. We investigate and quantify how sensitive such a participant’s pension outlook is to decisions made earlier in life, when decisions were based on a possibly wrong assessment of risk preferences or of future pension contributions.

Our discussion in this paper starts with the individual participant, studying the importance of tailoring decisions to the participant’s specific situation and the costliness of “mistakes” due to changes in risk preferences or risk capacities. Aside from some important exceptions, we find that outcomes are surprisingly robust to deviations from the theoretically optimal strategy. Importantly, this robustness result is largely independent of the precise reason for a difference between the implemented strategy and the theoretical optimum. Besides changes in risk preferences or risk capacities, one can also

interpret our results in terms of (1) measurement errors in communicating preferences between the participant and the pension fund, (2) a pension fund grouping slightly different participants in a single risk class, or (3) young participants paying little attention to their pension investments – or a combination of these factors. Perfectly measuring a participant's old-age risk preferences and life-time risk capacity to fully personalize pension investments seems like a daunting task. This is even more the case because financial market conditions are only observed up to statistical error. Our results suggest that such full personalization may not be necessary.

As a first main finding, we see that following a (somewhat) suboptimal lifecycle for up to ten years hardly has an effect on welfare, as this can be counteracted by switching to the optimal lifecycle in time. Of course, the idea here is not to compensate overly risk-averse behavior in earlier periods by overly risky behavior later in life, or the other way around. What rather helps is that the amount invested in risky assets at early ages is limited due to leverage constraints, that a close-to-optimal investment fraction tends to give close-to-optimal results, and that a considerable part of the investment horizon is still left after ten or twenty years.

In fact, leverage constraints are key for ensuring that wealth cannot get (too) negative. Without such constraints, agents who overestimate their human capital (i.e., their future pension contributions) or underestimate their risk aversion may invest too riskily and end up in a situation from which they cannot recover without financial help.<sup>1</sup> Under leverage constraints, the possible welfare losses from working with a wrongly estimated risk aversion or wrongly estimated human capital are limited. Underestimation of risk aversion leads to excessively risky investments – but only to the point allowed by the leverage constraint. Potential losses from overestimation of risk aversion (or underestimation of human capital) are also limited as the investment mix converges to completely risk-free investment. In line with Joseph et al. (2021), we often observe that losses increase more slowly when risk aversion is overestimated rather than underestimated. However, this is not a general result. There are also cases where the absolute loss due to taking too little risk is larger.<sup>2</sup>

Next, we perform a sensitivity analysis with respect to financial market assumption, varying, in particular, the expected return on risky investment. With a higher expected return, the target fraction of risky investment is higher. Thus, in combination with hu-

---

<sup>1</sup>The Future of Pensions Act (Wet Toekomst Pensioenen) distinguishes between a solidarity scheme and a flexible defined contribution scheme (see Nijman (2022) for an overview). In the solidarity scheme, a leverage position up to 150% will be allowed. When leveraging is allowed and rebalancing happens in discrete time, wealth can become negative. However, pension wealth is not allowed to be negative at any time. The solidarity reserve could in such case ensure that pension wealth remains positive.

<sup>2</sup>For examples, see the left plots in Figures 4b, 5, 6a and 9a.

man capital, there is a more restricted investment trajectory due to leverage constraints being more binding. In this context, we also demonstrate a well-known fact from the literature on quantitative finance: estimating the expected return without access to centuries of data leads to considerable remaining uncertainty about expected returns and thus about the optimal investment fraction. From a quantitative perspective, this type of uncertainty will often be greater than the uncertainty in risk preferences or risk capacity.

Lastly, we show the sensitivity to different shapes of income (and contribution) trajectories over the lifecycle. In our baseline model, we allow for relatively drastic mistakes in estimated human capital – such as a participant wrongly expecting pension contributions to triple at some point. With more realistic amounts of uncertainty about income trajectories, we find much smaller welfare losses. Incorrect estimation of one's risk aversion by a factor two or three seems a more realistic threat compared to similarly drastic mistakes in assessing one's future income.

A key lesson we can draw is that an unexpected drop in pension contributions, such as due to disability, can go together with severe *additional* welfare losses when investment behavior had been too aggressive. Such a drop in pension contributions can also arise from becoming self-employed and thus leaving the mandatory participation in pension saving – or from any other reason that causes a switch from active to “sleeper” status. Trivially these effects are smaller when the unexpected drop in pension contributions is smaller. Such a drop could result from a divorce, a switch to a part-time job, becoming partially self-employed, or loss of a job.

The type of sensitivity analysis we conduct in this paper has some natural limitations. We can examine some sources of suboptimal decisions but never at all of them. Moreover, by settling on one particular relatively simple model, some potential threats will not be covered by our analysis. We mention some of them here. First, our financial market model assumes constant investment opportunities, constant interest rates, and abstracts from inflation. Second, on the individual preference side, we only consider utility functions with different levels of constant relative risk aversion (CRRA). We do not consider other utility functions or preferences outside the expected-utility paradigm such as habit formation, regret, loss aversion, or cumulative prospect theory. Each of these factors can potentially lead to welfare losses that our current analysis does not account for.

This paper lies at the intersection of two larger streams of related work in the pensions literature, namely research on empirical elicitation of preferences and research on optimal investment for individuals with heterogeneous and potentially uncertain risk preferences. See Bokern et al. (2021) and Alserda et al. (2019) among others for references to the former category on preference elicitation methodologies. A particularly



related project is recent work by Bokern et al. (2022) on the dynamics of risk attitudes. Our research can be thought of as adding the next steps from dynamic preference trajectories to decisions. In the second category, there are studies by Joseph et al. (2021), Alserda et al. (2019), Balter and Schweizer (2021), and Balter et al. (2022). While these projects focus on heterogeneity in the cross-section of participants at a given point in time, the focus of our research is on heterogeneity over time for a fixed participant. Introduction of another time dimension through the evolution of human capital gives rise to lifecycle theory. We explicitly model the evolution of salaries and human capital in the investment problem we consider. Our paper thus also belongs to the literature on lifecycle investment; see Bodie et al. (1992), Campbell et al. (2001) and Cocco et al. (2005) for seminal contributions in that area.

The paper is organized as follows: Section 2 presents the model, while Section 3 presents the results. Section 4 discusses some practical challenges and Section 5 contains our conclusions.

## 2 The setting

### 2.1 Financial Market

There is a risky asset with price process  $S_t$  over a time horizon  $[0, T]$ . The dynamics of  $S_{t_{i+1}}$  are given by

$$S_{t_{i+1}} = S_{t_i} e^{\mu\Delta - \frac{1}{2}\sigma^2\Delta + \sigma\Delta W_{t_{i+1}}}, S_{t_0} = 1, \quad (1)$$

where  $\mu$  and  $\sigma$  are positive constants and  $\Delta W_{t_{i+1}}$  is a Brownian motion increment with mean zero and variance  $\Delta$ . Thus,  $S_t$  follows a geometric Brownian motion. Time is discretized in  $M$  steps where  $t_i = i\Delta$ ,  $\Delta = \frac{T}{M}$  implying  $t_0 = 0$  and  $t_M = T$ . Our results are all based on a sample of  $N = 10,000$  scenarios drawn from this model.

We consider an investor who maximizes expected utility from terminal wealth at time  $T$  by trading in the risky asset  $S$  and in a riskless asset  $A$ . The latter evolves by

$$A_{t_{i+1}} = A_{t_i} e^{r\Delta}. \quad (2)$$

We now revisit the classical portfolio choice problem, i.e., the Merton problem, where  $V_T$  is the terminal wealth. Denoting by  $m_t^V$  the fraction of wealth invested in the risky asset at time  $t$ , the dynamics of  $V_t$  are given by

$$V_{t_{i+1}} = (1 - m_{t_i}^V) e^{r\Delta} V_{t_i} + m_{t_i}^V \frac{S_{t_{i+1}}}{S_{t_i}} V_{t_i}. \quad (3)$$

The investor maximizes the objective

$$\max_{(m_{t_i}^V)_i} E[u(V_T)], \quad (4)$$

where we assume that utility  $u$  is a CRRA function,

$$u(x) = \begin{cases} \frac{x^{1-\gamma}}{1-\gamma} & \gamma > 1 \\ \ln x & \gamma = 1, \end{cases} \quad (5)$$

and where  $\gamma$  captures the constant relative risk aversion  $-x \frac{u''(x)}{u'(x)}$ . This is equivalent to solving

$$\max_{(m_{t_i}^V)_i} CE^\gamma(V_T) = \max_{(m_{t_i}^V)_i} u^{-1}(E[u(V_T)]), \quad (6)$$

where  $CE^\gamma(V_T)$  denotes the certainty equivalent of terminal wealth  $V_T$ . It is well-known that in the continuous time limit,  $\Delta \rightarrow 0$ , the optimal investment fraction is

$$\bar{m}_{t_i}^V = \frac{\mu - r}{\sigma^2 \gamma}. \quad (7)$$

This is also known as the Merton fraction. In the pension context that we consider here, terminal time  $T$  denotes the moment of retirement, time is counted in years, and time 0 is the start of the planning horizon. The investor can be thought of as a participant in a pension product offered by a pension fund or insurer. The pension fund or insurer executes the trading (and thus the utility maximization) on behalf of the participant. We thus also call the investor the “participant” or, simply, the “agent”. Wealth  $V$  can be thought of as the total *pension* wealth. The latter consists of yearly contributions that are proportional to one’s salary. Total pension wealth can be subdivided into two categories, financial wealth  $F_t$  and human capital  $H_t$ :

$$V_{t_i} = F_{t_i} + H_{t_i}. \quad (8)$$

The annualized pension contribution in period  $t$  is denoted by  $h_t$ . This is equivalent to an actual contribution of  $h_t \Delta$  in period  $t$ . The fraction of *financial* wealth that is invested in the risky asset  $S$  is denoted by  $m_t$ . Together this implies the following dynamics of financial wealth

$$F_{t_{i+1}} = (1 - m_{t_i})e^{r\Delta}F_{t_i} + m_{t_i}\frac{S_{t_{i+1}}}{S_{t_i}}F_{t_i} + h_{t_i}\Delta e^{r\Delta}. \quad (9)$$

Thus, in every period of length  $\Delta$ , the pension account is invested for  $m_{t_i}$  in the risky asset,  $1 - m_{t_i}$  on the bank account, and the pension contribution  $h_{t_i}\Delta$  is added at the beginning of the period and assumed to be invested on the bank account throughout the period. Alternatively, this can be interpreted such that the contribution  $h_{t_i}\Delta e^{r\Delta}$  is added to the pension account at the end of the period.

We assume that labor income is independent of developments in financial markets. Moreover, we assume salary to be deterministic. Human capital is defined as the present value of all future premium contributions,

$$H_{t_i} = \sum_{j=i}^{M-1} h_{t_j} e^{-r(j-i)\Delta}. \quad (10)$$

The amount of human capital affects how much an investor is willing to invest via the magnitude and riskiness of his or her *total* wealth, i.e., the sum of current financial wealth and human capital,  $V_{t_i} = F_{t_i} + H_{t_i}$ . At the moment of retirement, human capital equals zero

$$H_T = 0 \quad \text{and thus} \quad V_T = F_T. \quad (11)$$

The dynamics of  $H_{t_i}$  can also be expressed by the recursive formulation

$$H_{t_i} = e^{-r\Delta}H_{t_{i+1}} + h_{t_i}\Delta. \quad (12)$$

Finally, note that only  $F$  is directly observed in practice. In contrast,  $H$  and  $V$  can only be best estimates based on future pension contributions.

The dynamics of  $F_t$ ,  $A_t$  and  $V_t$  imply that any investment fraction  $m_t$  based on  $F$  can be translated into an investment fraction  $m_t^V$  based on  $V$  using the formula

$$m_{t_i} = m_{t_i}^V \frac{F_{t_i} + H_{t_i}}{F_{t_i}}. \quad (13)$$

As we are trading in discrete time, both  $F$  and  $V$  could become negative in case of leveraging. Mathematically, what we need to guarantee for our model to be well-defined is that terminal wealth  $V_T = F_T$  is positive because otherwise  $u(V_T)$  is negative infinity. To achieve this, one needs to ensure that the investment fraction  $\bar{m}_{t_i}^V$  defined in (7) satisfies

$$0 \leq \bar{m}_{t_i}^V \leq 1. \quad (14)$$

All scenarios studied in this paper are such that (14) holds. Participants may thus want to leverage at the level of financial wealth,  $m_{t_i} > 1$ , but not at the level of total wealth, leading to possibly negative values of  $F_{t_i}$  at intermediate time points which are then compensated by later pension contributions. In line with existing policy regulations that try to limit the probability and extent of negative financial wealth, we assume that there is an upper bound  $m_{max} \geq 1$  on the maximum degree of leveraging with regard to financial wealth. We assume throughout that the fraction of financial wealth that is invested in the risky asset is chosen to reflect as closely as possible an investment under the Merton fraction on the level of total wealth,

$$\bar{m}_{t_i} = \min \left( m_{max}, \bar{m}_{t_i}^V \frac{F_{t_i} + H_{t_i}}{F_{t_i}} \right). \quad (15)$$

In our sensitivity analyses below, we consider situations in which investment decisions are based on misspecified values of  $H$  and  $\gamma$  (and thus  $\bar{m}_{t_i}^V$ ). In that case, we can still simulate the actual evolution of financial wealth by combining these misspecified investment fractions with the actual process of pension contributions. However, when the investment mix is based on overestimated values of the pension contributions  $h_{t_i}$ , it can happen that financial wealth becomes negative and the pension contributions are insufficient for keeping total wealth positive and, importantly, insufficient for a recovery at the end when  $F_T = V_T$  with probability 1. The problem is that, in order to check whether (14) is satisfied for a given choice of investment fraction  $m_{t_i}$ , one needs to compute the implied investment fraction at the level of total wealth,

$$m_{t_i}^V = m_{t_i} \frac{F_{t_i}}{F_{t_i} + H_{t_i}}. \quad (16)$$

Performing this calculation with an overestimated value for the future pension contribution  $H_{t_i}$  can lead to a false belief that  $m_{t_i}^V$  is low enough to satisfy (14) and keep total

wealth always positive. In principle, only a ban on leveraging,  $m_{max} = 1$ , can completely eliminate this possibility independently of  $h$ , implying that the right hand side of (16) is less than 1 for all  $H_{t_i} \geq 0$ . In this paper, we take a pragmatic approach to this problem: we fix our set of 10,000 simulated scenarios and note that for all combinations of  $h$  and  $m_{max}$  that we consider, terminal wealth is positive in all scenarios.<sup>3</sup>

As output measure we calculate the certainty equivalent as a function of  $(m_t)_t$ ,  $(h_t)_t$  and  $\gamma$ ,

$$CE(m, h, \gamma) = u^{-1} (E[u(F_T(m, h))]) = (E[F_T(m, h)^{1-\gamma}])^{\frac{1}{1-\gamma}}. \quad (17)$$

The certainty equivalent corresponds to the deterministic amount of money received at time  $T$  that the agent considers exactly as valuable as the stochastic payoff  $F_T(m, h)$ . The certainty equivalent under the strategy  $\bar{m}_{0,T}(h, \gamma)$  we denote by  $CE^*$ ,

$$CE^* = CE^*(\bar{m}_{0,T}(h, \gamma), h, \gamma) \quad (18)$$

where

$$\bar{m}_{0,T}(h, \gamma) = \left( \min \left( m_{max}, \frac{\mu - r}{\sigma^2 \gamma} \frac{F_{t_i} + H_{t_i}}{F_{t_i}} \right) \right)_{i=0}^{M-1}.$$

In the following, we study the reduction in the certainty equivalent that arises from using strategies  $m \neq \bar{m}_{0,T}(h, \gamma)$ .

## 2.2 Suboptimal Decisions

In our analysis, we mainly focus on two sources of suboptimal decision, namely misperceived (or changing) risk preferences and/or misperceived risk capacity, i.e., wrong projections of future pension contributions. We capture this by a simple “moment of truth” model: at some intermediate time point  $t$ , such as at age 40 or 50, the agent realizes that his or her investment strategy so far was based on a misperception of risk preferences or expected future earnings. Compared to more complex and thus possibly more realistic models, this model has two major advantages. First, it is simple and easy to interpret and understand. Second, it is relatively extreme and should thus give an upper bound on more continuous processes of adjusting beliefs.

In our baseline model, we assume that the true risk aversion is equal to  $\gamma$  and that the pension contributions are equal to  $h_0$  from time 0 to time  $t$  and equal to  $h_1$  from time  $t$  to  $T$ , reflecting an increase in salary along the career path. Under false beliefs, the risk aversion is equal to  $\tilde{\gamma}$  from time 0 to  $t$  and correct afterwards. Initially, the computation of overall human capital is based on the true  $h_0$  from time 0 to  $t$  and based on false

<sup>3</sup>In fact, as soon as terminal wealth is negative in a single scenario, expected utility jumps to  $-\infty$ , leading to trivial results.

expectations  $\tilde{h}_1$  for time  $t$  to  $T$ . At time  $t$  the agent realizes that his or her career trajectory does not lead to  $\tilde{h}_1$  but rather to  $h_1$ . From that time onwards, the agent calculates human capital based on  $h_1$ . The pension accruals are always based on the true contributions. However, it is the false expectation that causes suboptimal investment strategies.

Note that there is a slight asymmetry in how we model misperceptions about risk preferences and about risk capacity. For risk preferences, it is easy to conceive that an agent thinks for many years that his or her risk aversion is  $\gamma = 3$  even though it really is  $\gamma = 6$ . This is even more so because  $\gamma$  in the present context should be thought of as a best estimate of risk aversion at the moment of retirement at time  $T$ , not the current level of risk aversion. In contrast, it seems less realistic that agents would have strongly distorted perceptions of their current pension contributions. Consequently, we only allow for wrong beliefs about the future level of  $h$  but not about its current level.

To summarize the notation,

$$\gamma_{t_i} = \gamma \text{ for all } t_i \in [0, T] \quad (19)$$

$$\tilde{\gamma}_{t_i} = \begin{cases} \tilde{\gamma} & \text{if } t_i < t \\ \gamma & \text{if } t_i \geq t \end{cases} \quad (20)$$

$$h_{t_i} = \begin{cases} h_0 & \text{if } t_i < t \\ h_1 & \text{if } t_i \geq t \end{cases} \quad (21)$$

$$\tilde{h}_{t_i} = \begin{cases} h_0 & \text{if } t_i < t \\ \tilde{h}_1 & \text{if } t_i \geq t \end{cases} \quad (22)$$

$$H_{t_i} = \begin{cases} \sum_{j=i}^{t/\Delta-1} h_0 e^{-r(j-i)\Delta} + \sum_{j=t/\Delta}^{M-1} h_1 e^{-r(j-i)\Delta} & \text{if } t_i < t \\ \sum_{j=i}^{M-1} h_1 e^{-r(j-i)\Delta} & \text{if } t_i \geq t \end{cases} \quad (23)$$

$$\tilde{H}_{t_i} = \begin{cases} \sum_{j=i}^{t/\Delta-1} h_0 e^{-r(j-i)\Delta} + \sum_{j=t/\Delta}^{M-1} \tilde{h}_1 e^{-r(j-i)\Delta} & \text{if } t_i < t \\ \sum_{j=i}^{M-1} h_1 e^{-r(j-i)\Delta} & \text{if } t_i \geq t. \end{cases} \quad (24)$$

We denote the resulting suboptimal certainty equivalent by

$$\widetilde{CE} = CE \left( \left\{ \bar{m}_{0,t}(\{h_0, \tilde{h}_1\}, \tilde{\gamma}), \bar{m}_{t,T}(\{h_0, h_1\}, \gamma) \right\}, \{h_0, h_1\}, \gamma \right) \quad (25)$$

and calculate the relative loss by the certainty equivalent ratio, which is the certainty equivalent of the suboptimal investment relative to the optimal certainty equivalent

$$CE\text{-ratio} = \frac{\widetilde{CE}}{CE^*}. \quad (26)$$

This quantity is at most equal to 1 and can be interpreted as follows. When  $CE\text{-ratio} = 0.95$  this implies that the certainty equivalent is 5% lower than the certainty equivalent

that could have been attained under the optimal investment strategy. To put this number into further perspective, suppose that the optimal certainty equivalent corresponds to an annualized average growth rate  $\rho^*$ ,  $CE^* = V_0 \exp(\rho^*T)$ , while the suboptimal certainty equivalent corresponds to a reduced rate  $\tilde{\rho}$ ,  $\widetilde{CE} = V_0 \exp(\tilde{\rho}T)$ . Then, the reduction in rate,  $\delta = \rho^* - \tilde{\rho}$ , can be written as

$$\delta = \frac{1}{T} \log(CE\text{-ratio})$$

Consequently, for an investment horizon of forty years,  $T = 40$ , a  $CE$ -ratio of 0.95 corresponds to a reduction in the yearly growth rate by  $\delta = 0.13\%$ , while for  $T = 20$  we find  $\delta = 0.26\%$ . Another interpretation of the  $CE$ -ratio is based on reduced pension contributions:  $CE\text{-ratio} = 0.95$  implies that  $\widetilde{CE}$  is as good as reducing all contributions as well as initial financial wealth by 5% and then investing in the optimal way.<sup>4</sup>

---

<sup>4</sup>Whether a given level of welfare loss is small or large is highly subjective – and we would not want to prescribe a fixed cutoff value. To simplify the discussion below, we call losses that are less than 1% small and losses that are higher than 20% substantial. We leave it to the reader to decide where the precise cutoff for adverse outcomes should be.

### 3 Results and discussion

#### 3.1 Outline, Scenarios and Parameters

We are now ready to compute the relative losses due to suboptimality caused by wrong preference estimation, wrong salary expectations, or both. We begin with an overview of the different scenarios that we will study. In Subsection 3.2, we then consider our baseline scenario in detail. In Subsection 3.3, we consider different choices of the true parameters with respect to risk aversion and risk capacity. Next, in Subsection 3.4 we discuss the robustness of our results to financial market conditions. In Subsection 3.5, we vary the timing of the “moment of truth” when the agent realizes the true parameters, and in Subsection 3.6 we consider alternative labor income assumptions that reflect continuous wage growth rather than a one-time jump. Finally, in Subsection 3.7, we look at different bounds on the ability to leverage.

Throughout we assume the following set of parameters:  $T = 40$ ,  $M = 120$ ,  $\Delta = \frac{1}{3}$ , and  $h_0 = 1$ . This reflects an individual aged 27 who retires at age 67. As our benchmark, we choose scenario  $Z_1$  as shown in the first row of Table 1. We assume a true risk aversion equal to  $\gamma = 3$ , which is within the typical 1 – 10 range found in the literature.<sup>5</sup> The yearly pension contribution is normalized to  $h_0 = 1$ , which after  $t$  years grows with a factor 2 to  $h_1 = 2$ . In line with the Dutch solidarity pension contribution scheme, we allow for 50% leverage, thus  $m_{max} = 1.5$ . Moreover, the parameters in the financial market are  $\mu = 0.04$ ,  $r = 0.01$  and  $\sigma = 0.2$ . To avoid a strong demand for excessive leverage at the start of the investment horizon, we set  $F_{t_0} = 1$  so that the initial capital is already equal to one year of pension contributions. Moreover, we choose  $t = 20$ , moving the moment of truth, at which the agent aligns the investment strategy with the true preferences and true income trajectory, to age 47.

In Table 1, we introduce eight alternative scenarios including different values for the true parameters  $(\gamma, h_1)$  in scenarios  $Z_2$ - $Z_5$ , a different timing of the moment of truth  $t$  in scenarios  $Z_6$  and  $Z_7$ , and different bounds on the degree of leveraging ( $m_{max}$ ) in scenarios  $Z_8$  and  $Z_9$ . In the later sections, we assume that one of these scenarios is the truth but that the agent is not aware of this initially. For instance, in  $Z_5$  the agent will suffer from disability and not make any additional pension contributions after time  $t$ ,  $h_1 = 0$ . However, until time  $t$  the agent is not yet aware of this problem and invests according to a different expectation  $\tilde{h}_1$  about future pension contributions. Our analysis then focuses on studying the *CE-ratios* introduced before: we ask how much the agent could have gained from an improved financial planning due to having a perfect assessment of his or her future pension contributions. This type of question we ask for all the different

<sup>5</sup>See for instance Conine et al. (2017) and the references therein.



Table 1: Overview of scenarios

	$Z_i, i =$	$T$	$t$	$\gamma$	$h_0$	$h_1$	$m_{max}$	$CE^*$
Base	1	40	20	3	1	2	1.5	84.3
Risk aversion up	2	40	20	<b>5</b>	1	2	1.5	80.0
Human capital up	3	40	20	3	1	<b>3</b>	1.5	109.9
Income drop	4	40	20	3	1	<b>1</b>	1.5	58.6
Disability	5	40	20	3	1	<b>0</b>	1.5	32.6
Early $t$	6	40	<b>10</b>	3	1	2	1.5	99.0
Late $t$	7	40	<b>30</b>	3	1	2	1.5	71.0
No leverage	8	40	20	3	1	2	<b>1</b>	83.9
Leverage up	9	40	20	3	1	2	<b>2</b>	84.5

scenarios, and we ask it both for contributions (and thus risk capacity) and for risk preferences.

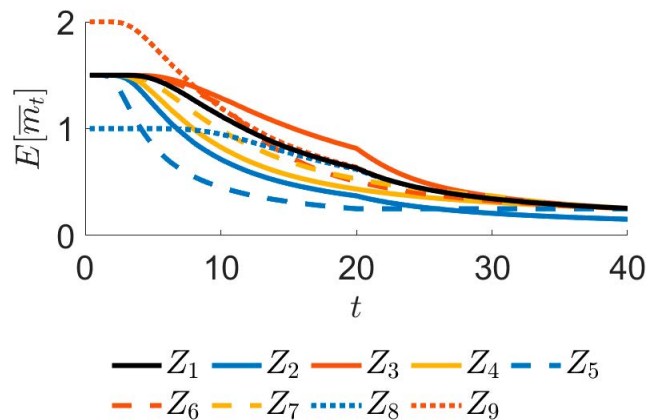
Before we start this *within-scenario* analysis, it may be instructive to compare the scenarios themselves. The final column of Table 1 shows the certainty equivalents  $CE^*$  introduced in (18) that result from optimal behavior in each scenario. These numbers thus translate the agent's overall utility in the different scenarios into comparable monetary amounts. Compared to the baseline  $Z_1$ , what we see in scenarios  $Z_2$ - $Z_5$  is quite intuitive: the certainty equivalent goes up with higher contributions and down with lower ones. Moreover, it goes down with a higher risk aversion because a more risk-averse agent gets less utility from any lottery. Shifting the timing of  $t$  in  $Z_6$  and  $Z_7$  is more meaningful in the later analysis when it corresponds to the end of suboptimal behavior. For the moment, an earlier  $t$  means in particular that the event where  $h$  doubles is earlier, corresponding to higher human capital and thus a higher certainty equivalent. The last two lines of the table are more interesting: we see that in the economic scenario under consideration, moving from no leveraging (and thus ruling out negative financial wealth) to  $m_{max} = 2$  (allowing agents to invest twice their financial wealth in the stock market) only increases the certainty equivalent by less than 1% while introducing a positive probability of negative financial wealth.

Another way to compare the scenarios and illustrate their diversity is by looking at optimal investment behavior. In Figure 1 we show the mean optimal strategies  $E[\bar{m}_t]$  over time for all nine scenarios. We take the mean because investment trajectories are stochastic since  $m_t$  depends on the state of both financial wealth and human capital. To give some indication of the volatility, Figure 2 compares the median glide path to the

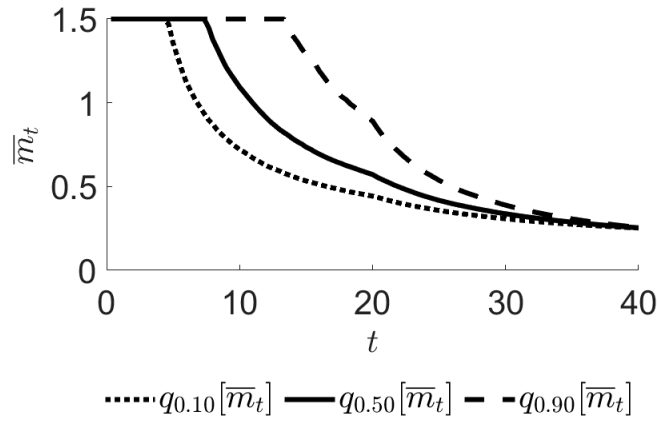
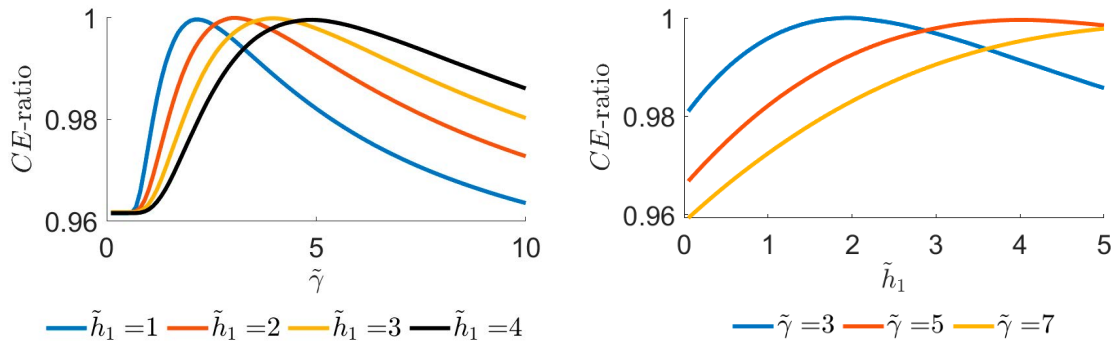
10%- and 90%-quantiles for scenario  $Z_1$ . Clearly, a trajectory that stays at the level  $m_{max}$  for a longer period corresponds to a less favorable financial market scenario, because financial wealth is still relatively small compared to human capital. We see that under the 90%-quantile the constraint remains binding for about nine years longer than under the more favorable 10% quantile.

In the base scenario, the true risk aversion level is 3, while the true income level is 1 during the first 20 years and 2 during the last 20 years. This is the black curve in the figure. In the alternative scenario  $Z_2$ , the investor's willingness to take risks is smaller,  $\gamma = 5$ , which leads to a lower investment curve as shown in blue. In the initial periods, however, the leverage constraint  $m_{max} = 1.5$  is binding in both scenarios so that the curves are flat and coincide. Later on, human capital diminishes and the difference between total wealth and financial wealth gradually disappears, so that the curves are sloping downward, ultimately converging to the Merton fraction which is 0.15 in scenario  $Z_2$  and 0.25 in all other scenarios.<sup>6</sup> In scenarios with higher human capital, we observe a stronger demand for leverage and thus higher curves. The opposite holds for the disability scenario  $Z_5$  shown in dashed blue. Finally, shifting the leverage constraint in scenarios  $Z_8$  and  $Z_9$  has the expected effect on investment fractions in the initial periods.

Figure 1: Average glide paths in different scenarios



<sup>6</sup>In particular, as long as an agent's perceived risk aversion  $\tilde{\gamma}$  lies in the range from 1- 10, the agent will want to invest at most 75% of his or her total wealth in the risky asset so that demand for leveraging is restricted to financial wealth.

Figure 2: Quantiles of glide path for scenario  $Z_1$ 

 Figure 3: Base scenario  $Z_1$ ,  $T = 40$ ,  $t = 20$ ,  $\gamma = 3$ ,  $h_0 = 1$ ,  $h_1 = 2$ ,  $m_{max} = 1.5$ .


### 3.2 The baseline scenario

In Figure 3, we show the certainty equivalent ratios

$$CE\text{-ratio} = \frac{\widetilde{CE}}{CE^*}$$

as functions of  $\tilde{\gamma}$  for four different estimations of future contributions on the left, and on the right as a function of  $\tilde{h}_1$  for three different levels of risk aversion. Thus, in the left panel, the red curve corresponds to the case where beliefs about future contributions are correct,  $\tilde{h}_1 = h_1 = 2$ , and the belief about risk preferences is on the  $x$ -axis. The  $CE$ -ratio is maximal around the true value  $\tilde{\gamma} = \gamma = 3$ . Moving away in either direction leads to a utility loss. The other curves correspond to different values of  $\tilde{h}_1$ . Conversely, in the right panel, the blue curve corresponds to correct beliefs about risk aversion,  $\tilde{\gamma} = \gamma = 3$ , and it is maximal around the point where future pension contributions

sion,  $\tilde{\gamma} = \gamma = 3$ , and it is maximal around the point where future pension contributions are assessed correctly,  $\tilde{h}_1 = h_1 = 2$ . As a first main take-away from this picture, we see that all curves stay above 0.96 at all points – despite the considerable range of false beliefs under display.

The leverage constraints are a big part of the reason for this robustness. Because leveraging is bounded, the loss due to an underestimation of the true risk aversion parameter is limited. The smaller the perceived risk aversion, the more the investor would mistakenly want to invest in risky assets. However, since this is bounded, the loss is bounded too, and all curves are flat for small  $\tilde{\gamma}$  where the constraint is binding. On the other hand, when the agent overestimates the true risk aversion level, then he or she will take less risk than what would be optimal, which lowers the relative utility. In this particular setting, we observe that a perceived risk aversion level that is too low – and following the resulting too risky strategy – leads to a certainty equivalent loss of at most 4%. When the strategy is too conservative, the loss depends on the future income assessment. When the human capital is estimated correctly, the loss is less than 3% for  $\tilde{\gamma} = 10$ . An overestimation of future income can counterbalance an overestimation of the risk aversion because overestimation of future contributions leads to excessive investment in risky assets, while overestimating the risk level leads to too little exposure.

When the risk aversion is overestimated, the loss is also bounded as in the limit nothing is invested riskily. Thus, when pension wealth is completely invested on the bank account against the risk-free rate, namely, when  $\tilde{\gamma} \rightarrow \infty$  then  $m_{t_i} \rightarrow 0$  irrespective of  $\tilde{h}_1$ . This loss is at its highest when  $t = T$ , i.e., the suboptimal strategy is followed until the end, thus until the wrong preference estimation is only realized at retirement. In that case the certainty equivalent is simply  $\widetilde{CE} = (H_{t_0} + F_{t_0})e^{rT}$  which leads, under the optimal investment decision in scenario  $Z_1$ , to a  $CE$ -ratio of 0.87.

For our comparative studies here and later on, we need to fix ranges over which the agent's false beliefs  $\tilde{\gamma}$  and  $\tilde{h}_1$  vary. For the risk aversion parameter  $\tilde{\gamma}$ , a natural range is the range from 1 to 10 discussed above. For  $\tilde{h}_1$  (and also for the human capital process  $(h_t)$ ) we deliberately use relatively extreme scenarios regarding the growth of pension contributions and the mistakes that agents can make when assessing their future pension contributions. The goal here is to find the order of magnitude where variations in risk aversion and variations in risk capacity have a comparable impact. In Section 3.6, when looking at more realistic cases for the evolution of pension contributions, we find that, encouragingly, the quantitative impact is much smaller. This leads to the tentative conclusion that wrong assessments of contribution payments have a smaller impact than wrong assessments of risk preferences. Finally, the left panel of Figure 3 illustrates that the interplay between misestimation of both  $\gamma$  and  $h_1$  plays a crucial role: for each of the  $\tilde{h}_1$ -values under consideration, there is a value of  $\tilde{\gamma}$  that gives a near-optimal  $CE$ -ratio

close to 1. Yet, similarly, mistakes made in the assessment of the two quantities can also reinforce each other.

### 3.3 Alternative scenarios for risk aversion and risk capacity

In scenario  $Z_2$ , where the true level of risk aversion is not equal to 3 but equal to 5, we obtain Figure 4a. We see now that the lower limit in the left plot of Figure 4a is lower than in the base scenario, but that the losses for high levels of  $\tilde{\gamma}$  are less severe. In other words, the loss function shifts to the right together with the true value of  $\gamma$ .

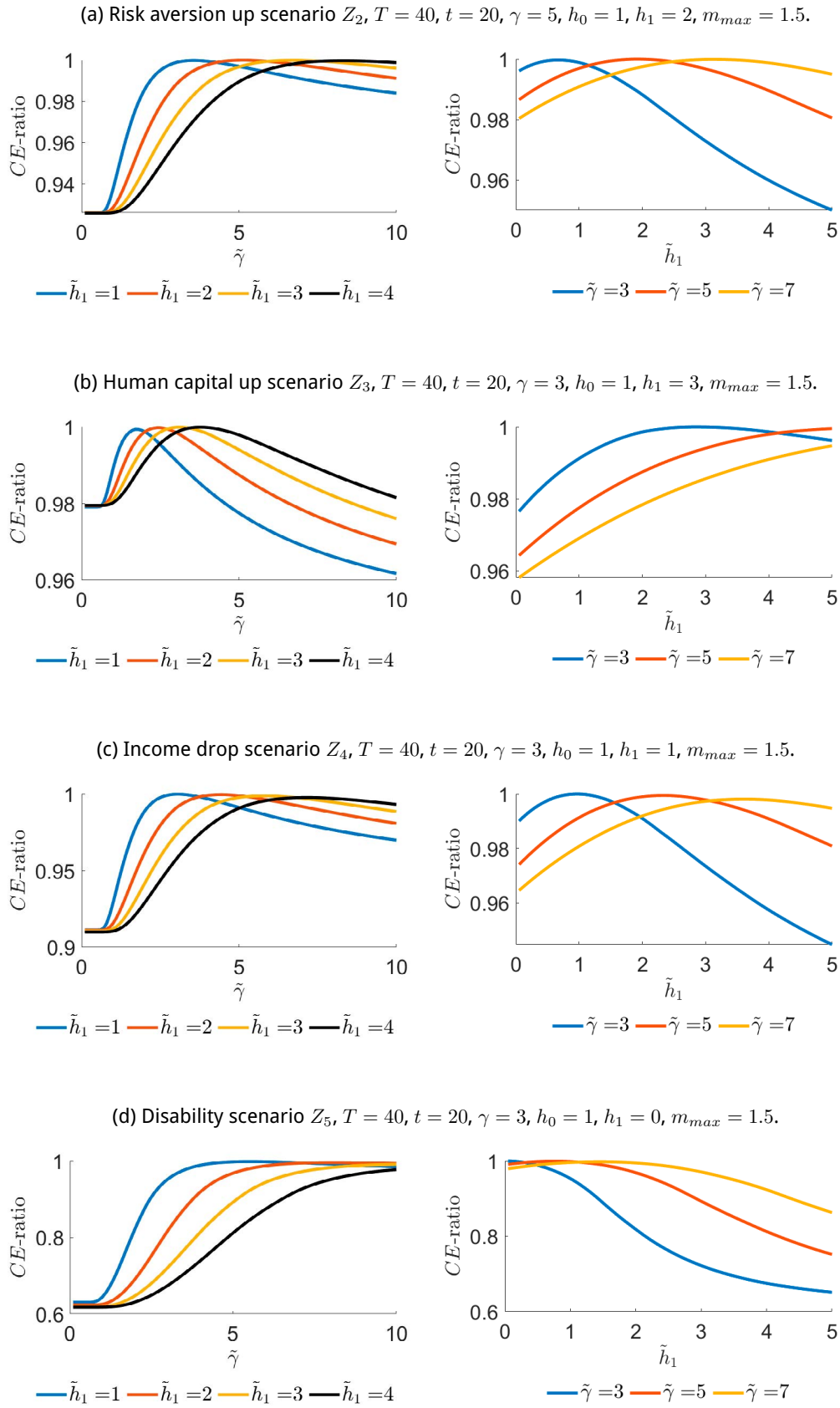
In scenarios  $Z_3$  to  $Z_5$  we consider different values of the true future pension contributions  $h_1$ . In  $Z_3$ , the true career path involves a tripling in income. Here we see in Figure 4b that underestimation of the risk level causes less severe losses than in  $Z_1$  because the true income is now higher. This implies that, in general, the target investment fraction is higher and thus the leverage constraint becomes more binding.

In Figure 4d we show the  $CE$ -ratio when income vanishes after 20 years, scenario  $Z_5$ . For example, one might think of a situation in which the agent becomes disabled. If this has not been anticipated while investing pension capital, the loss can be substantial, in particular when  $\tilde{\gamma}$  is low or when  $\tilde{h}_1$  is high. This means that taking too much risk can come at a high cost when future income disappears. Note that this welfare loss from an ex-post mismatch between realized and optimal investment strategy comes *on top of* the welfare loss from the disability itself, which can be computed by comparing  $Z_1$  and  $Z_5$  in the final column of Table 1.

More generally, the realized income pattern in scenario  $Z_5$  corresponds to individuals leaving the pension systems, i.e., moving from active participant to sleeper. From the perspective of a pension provider, a drop in contribution payments from  $h_0 = 1$  during the first 20 years to  $h_1 = 0$  in the remaining 20 years can have several, very different but often unobserved causes including disability, but also becoming self-employed, becoming unemployed or, emigration. To react and differentiate optimally, pension providers would ideally have full information on the pension resources. For instance, in situations in which pension is accrued elsewhere this should be reflected in the risk exposure and risk capacity (see AFM (2023)).

In Figure 4c, we show what happens when  $h_1 = 1$ , scenario  $Z_4$ . This reflects a constant level of income, but compared to  $\tilde{h}_1 > 1$  it captures an unexpected decrease in pension contribution relative to what has been anticipated. This implies an interpolation between the previous two figures. Examples of this could be a drop in income because of divorce, partial unemployment, partial disability, or any other unforeseen life event that causes a drop in pension contributions.

Figure 4: Risk aversion and human capital



### 3.4 Financial market conditions

In this section, we briefly discuss how financial market conditions and, in particular, different values for the drift coefficient  $\mu$  influence our results. Arguably, the strongest assumption we make regarding financial market conditions is that they are perfectly known. We begin by making this point more concrete. From a statistical perspective,  $\mu$  is notoriously hard to estimate, see, e.g., Section 4.2 of Rogers (2013), who points out that hundreds of years of data might be needed to reliably pin down this parameter. This has some fairly important implications for our analysis as well. The one crucial place where (possibly mismeasured) risk aversion coefficients enter our decision-making process is in the computation of the Merton fraction

$$\widehat{m}^V = \frac{\widehat{\mu} - r}{\widehat{\sigma}^2 \widehat{\gamma}}.$$

Clearly, this quantity depends on the ratio of our estimated risk aversion  $\widehat{\gamma}$  and the notoriously inaccurate estimate of the excess return  $\widehat{\mu} - r$ . Intuitively, the noise in the ultimate decision  $\widehat{m}^V$  will reflect the noisiest of the three input quantities  $\widehat{\mu}$ ,  $\widehat{\gamma}$  and  $\widehat{\sigma}^2$ . From this perspective, we cannot expect large gains from aiming at *much* higher precision in the estimation of, e.g.,  $\gamma$  than we can expect in the estimation of  $\mu$ .

To illustrate this difficulty, we simulate 10,000 times 30 years of daily data (260 business days per year) and then estimate  $\mu$  and  $\sigma$  on each trajectory from the empirical mean and standard deviation of the logarithmic returns using (1). Table 2 gives some descriptive statistics for the resulting estimates of  $\mu = 0.04$ ,  $\sigma = 0.2$ , and  $(\mu - r)/\sigma^2 = 0.75$ , which is the optimal investment fraction of an agent with  $\gamma = 1$ . Here,  $q_\alpha$  denotes the  $\alpha$ -quantile.

Table 2: Estimating drift and variance

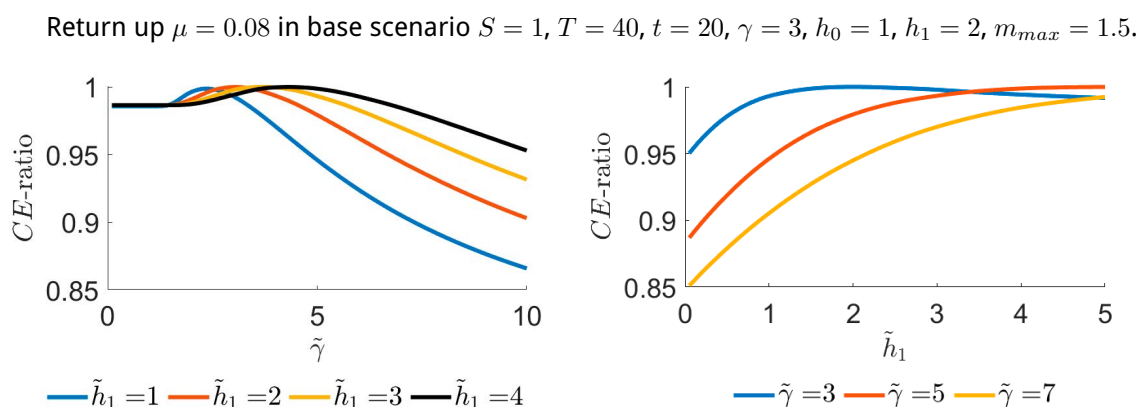
	min	$q_{0.05}$	$q_{0.25}$	$q_{0.5}$	mean	$q_{0.75}$	$q_{0.95}$	max
$\widehat{\mu}$	-0.1285	-0.0189	0.0153	0.0394	0.0397	0.0643	0.0993	0.1703
$\widehat{\sigma}$	0.1944	0.1973	0.1989	0.2000	0.2000	0.2011	0.2026	0.2064
$\frac{\widehat{\mu} - r}{\widehat{\sigma}^2}$	-3.5333	-0.7280	0.1330	0.7342	0.7438	1.3578	2.2264	4.0618

As expected, we see that the estimation of  $\sigma$  is fairly successful while there is considerable variation in the estimates of  $\mu$  and the resulting investment fractions. For instance, the estimated investment fractions in the 2,500 most conservative cases are more than a factor 10 smaller than the investment fractions in the 2,500 most aggressive cases, covering the entire range from keeping 87% of wealth in the risk-free asset to over-leveraging by 35%. This variation is purely due to the statistical error that is left after thirty years of

data. From this perspective, the additional noise that arises in the estimation of  $\gamma$  may have comparatively little impact on the noise in decisions. To end this discussion on a hopeful note, the literature on parameter uncertainty in the Merton problem<sup>7</sup> has shown that the problem is fairly stable in the sense that results stay close to optimal as long as investment fractions are not too far away from the optimum. In fact, also our previous robustness results for working with a misestimated  $\gamma$  can be directly translated into results about misestimating other components of the Merton fraction like the  $\mu$  – and vice versa.

Next, we consider how sensitive our main results are to changes in financial market conditions themselves. If we increase the expected return on the risky asset from  $\mu = 0.04$  to  $0.08$  while keeping all other things equal to the baseline scenario, then we see in Figure 5 that the losses are quite a bit larger and the leverage constraint is binding more often. One misses out on more, in particular when  $\tilde{\gamma}$  is high, now that the expected return is 8% rather than 4%.

Figure 5: Financial market



### 3.5 Shifting the “moment of truth”

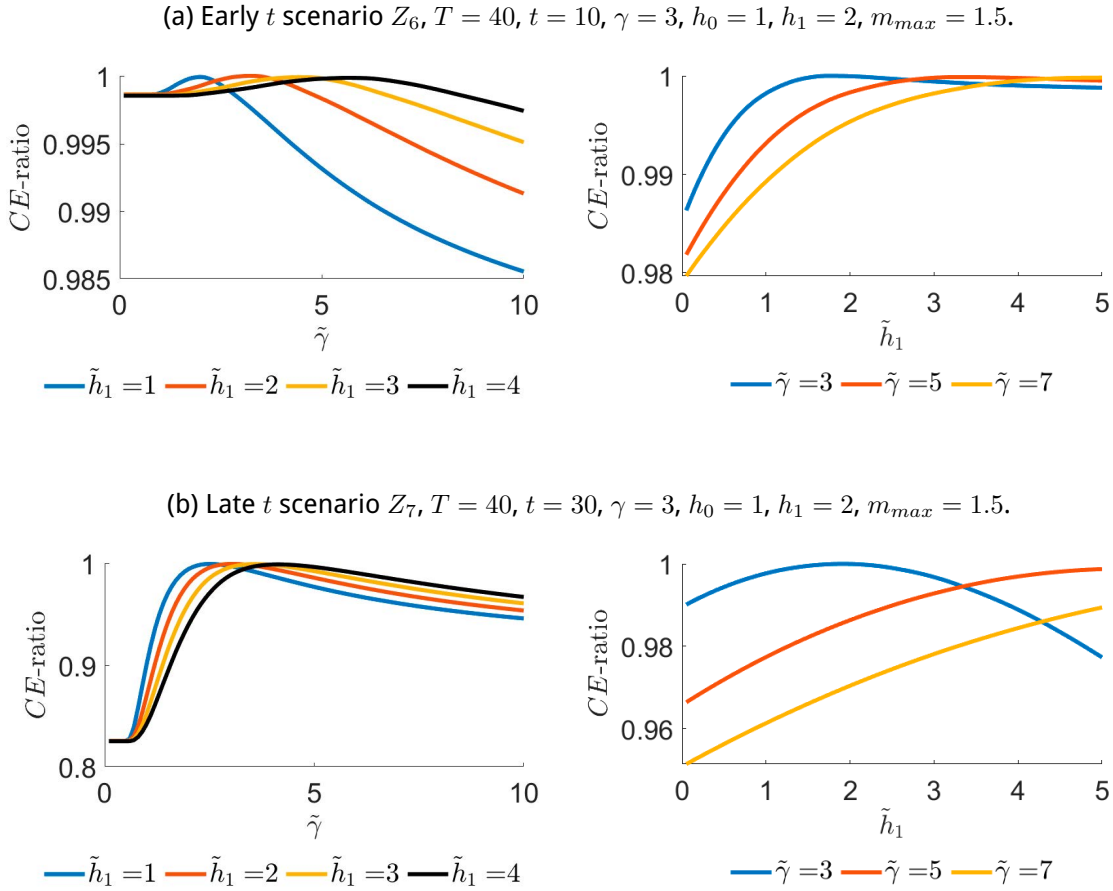
In Figure 6, we show the impact of being wrong about  $\gamma$  and  $h_1$  not until the age of 47 but until the ages of 37 and 57, respectively. As expected, the longer it takes to find out one’s true risk aversion and one’s true career path, the higher the loss because suboptimal strategies have been implemented for longer. Nevertheless, the figures can give us some quantitative idea on how much can be gained from learning one’s true old-age risk

<sup>7</sup>See e.g. again Rogers (2013), Chapter 2.32.



aversion a bit earlier, or from having an accurate estimate of one's overall career path a bit earlier.

Figure 6: Timing the moment of truth

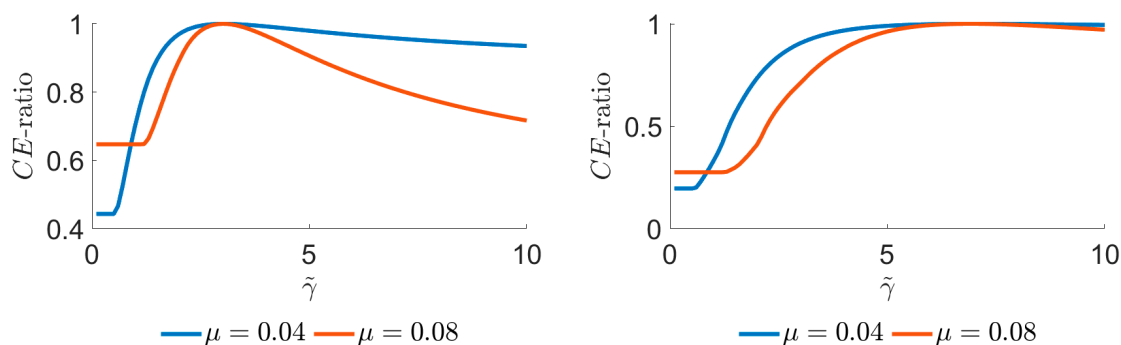


Finally, in Figure 7, we look at the even more extreme case that the moment of truth coincides with the moment of retirement – so that the entire investment strategy was based on parameters that differ from the true ones. In this case, it only makes sense to look at wrong beliefs about risk aversion  $\tilde{\gamma}$ : there is no time left between  $t$  and  $T$  so that  $\tilde{h}_1$  drops out of the calculation. A motivation for considering  $t = T$  could be the idea that the moment of retirement itself affects risk preferences so that agents can only learn their risk aversion accurately when the build-up phase of their pension wealth is over. Another interpretation would be that  $\tilde{\gamma}$  is the implemented risk aversion in a participant's pension account, which differs from the true  $\gamma$ , e.g., because communication between the participant and the pension provider is noisy, or because the pension provider combines participants with similar  $\tilde{\gamma}$  in a single risk class with the same investment strat-

egy. In both figures, we see that there is an interval around the true risk aversion level, which guarantees close to optimal results. This interval is wider when  $\mu$  is smaller. However, substantial welfare losses are possible when there is a stronger mismatch between the optimal and the implemented investment strategy over the entire investment horizon. Some additional discussion in this direction can be found in Sections 4 and 5 of Balter and Schweizer (2021), who investigate the welfare effects of offering only a limited number of investment fractions to a population of agents with heterogeneous risk preferences. Their results include bounds on how close a menu with a finite number of products comes to the full personalization optimum and heuristics for how to choose a menu of  $\gamma$ -levels.

Figure 7: The case  $t = T$

The case  $t = T = 40$  for  $\mu = 0.04$  (blue curves) and  $\mu = 0.08$  (red curves) under a true risk aversion of  $\gamma = 3$  (left panel) and  $\gamma = 7$  (right panel) with  $h_0 = 1$ ,  $m_{max} = 1.5$ .



### 3.6 Patterns of wage growth

So far, we have looked at relatively extreme scenarios for wage growth where pension contributions would double, triple or even vanish at some point in time ( $Z_3$ - $Z_5$ ). The motivation behind this was to study how much we need to shock the contribution process to get sizable effects. In this section, we round up this analysis by verifying that for more realistic patterns of wage growth the quantitative impacts are much smaller.

In order to build more realistic wage (and contribution) profiles, we use a stylized scheme which is known as the “3 – 2 – 1 – 0” scheme. This is a simple age-dependent pattern, where wage growth is 3% up until age 35, then 2% in the ten years until age 45, then 1% in the ten years until age 55, and 0% thereafter. Let  $g_{t_i}$  be the yearly rate at which contributions grow: per time step  $\Delta$ , contributions grow with rate  $(1 + g_{t_i})^\Delta$ . Under

false beliefs, the human capital is based on the true contribution path  $h_{t_i}$  until time  $t$  and based on false contributions  $\tilde{h}_{t_i}$  after time  $t$ . The present value of the “wrong” human capital is based on these discounted contributions until time  $t$ , after which the agent realizes that the contributions are different and adapts his or her false expectation to the true  $h_{t_i}$  after  $t$ . Overall, human capital is described by the following equations, where  $\tilde{g}_{t_i}$  denotes the false growth rate in income:

$$h_{t_0} = 1 \quad (27)$$

$$h_{t_i} = h_{t_{i-1}} \cdot (1 + g_{t_{i-1}})^\Delta \quad (28)$$

$$\tilde{h}_{t_i} = \begin{cases} h_{t_i} & \text{if } t_i \leq t \\ \tilde{h}_{t_{i-1}} \cdot (1 + \tilde{g}_{t_{i-1}})^\Delta & \text{if } t_i > t \end{cases} \quad (29)$$

$$H_{t_i} = e^{-r\Delta} H_{t_{i+1}} + h_{t_i} \Delta \quad (30)$$

$$\tilde{H}_{t_i} = \begin{cases} e^{-r\Delta} \tilde{H}_{t_{i+1}} + \tilde{h}_{t_i} \Delta & \text{if } t_i < t \\ H_{t_i} & \text{if } t_i \geq t \end{cases} \quad (31)$$

and where

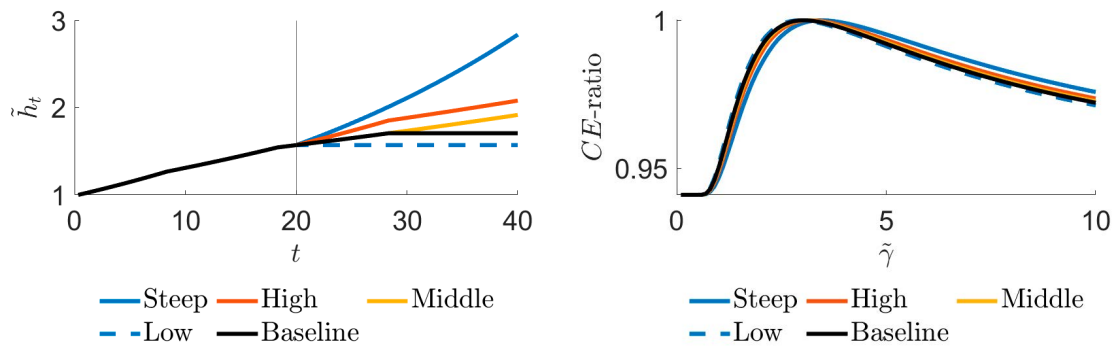
$$g_{t_i} = \begin{cases} g_0 & \text{if } 27 + t_i \leq 35 \\ g_1 & \text{if } 35 < 27 + t_i \leq 45 \\ g_2 & \text{if } 45 < 27 + t_i \leq 55 \\ g_3 & \text{if } 27 + t_i > 55 \end{cases} \quad (32)$$

For  $T = 40, t = 20, \gamma = 3, h_0 = 1, m_{max} = 1.5$  we consider the profile  $3 - 2 - 1 - 0$  as the new baseline scenario  $Z_{10}$ . As alternatives, we consider steeper and flatter wage profiles as described in Table 3 and the left plot in Figure 8, with the resulting  $CE$ -ratios shown on the right. In all these scenarios, the true growth curve of pension contributions is the same and identical to the baseline  $Z_{10}$ . The only difference is that until time  $t$  the agents behave as if they were on one of the other curves.

The blue line reflects expectations in line with a typical career path in the highest-achieving group (Lever et al. (2013)). Due to unforeseen circumstances, the anticipated increase in income is not achieved and the agent drops to the baseline curve. Examples might be failing to become medical specialist or a judge, occupations with long periods of education and development. In contrast, the dashed blue line reflects the wrong expectation that no career development will occur, reflecting, for example, an employee is promoted to a management position despite lower personal expectations. These differences in career paths seem to lead to only minor effects. More dispersion in income is needed to cause sizable impact, as we have seen in the previous sections.

Table 3: Wage profiles

Income growth	$Z_i, i =$	$\tilde{g}_0$	$\tilde{g}_1$	$\tilde{g}_2$	$\tilde{g}_3$
Baseline	10	0.03	0.02	0.01	0.00
Steep	10a			0.03	0.03
High	10b			0.02	0.01
Middle	10c			0.01	0.01
Low	10d			0.00	0.00

Figure 8: Income growth 3 – 2 – 1 – 0 based on scenario  $Z_{10}$  and alternatives as depicted in Table 3

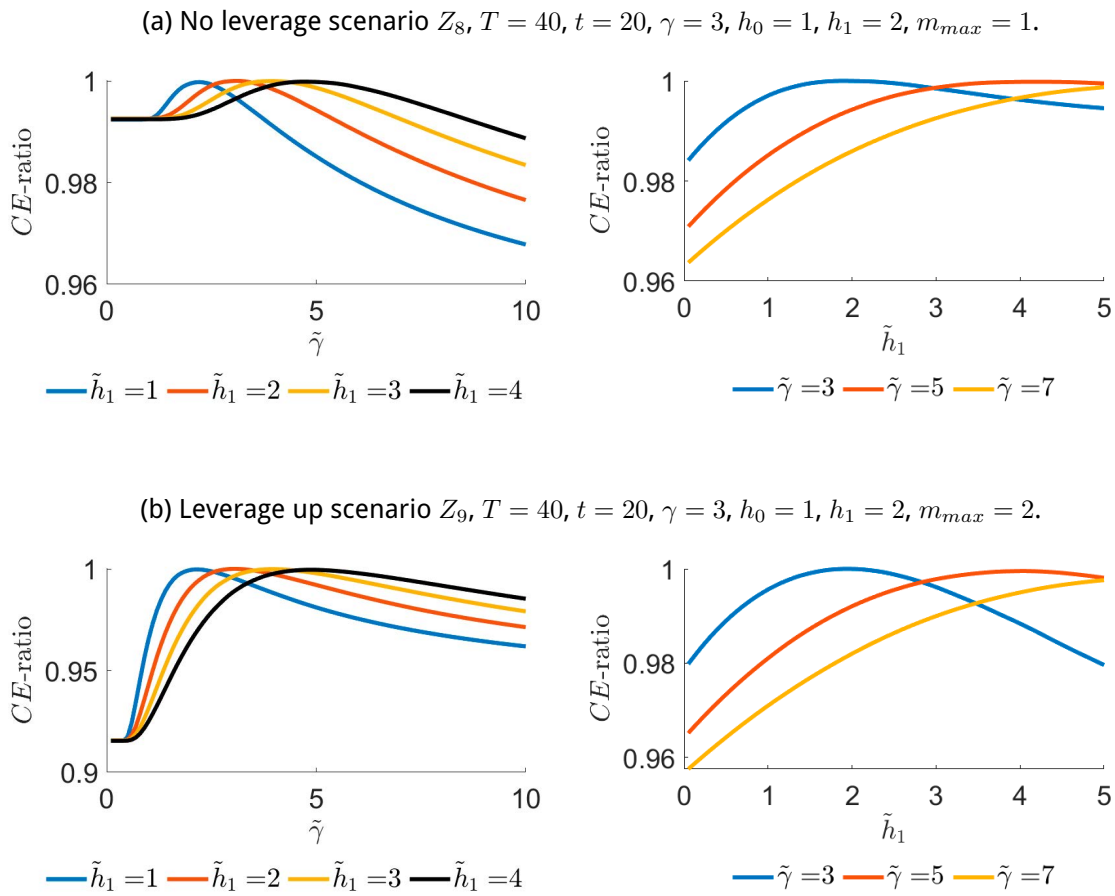
### 3.7 Leverage

We finally have a look at scenarios  $Z_8$  and  $Z_9$ , which vary the leverage constraint  $m_{max}$  compared to the baseline value of  $m_{max} = 1.5$  from scenario  $Z_1$ .<sup>8</sup> One important observation was already made earlier in the context of Table 1, namely that the welfare gains from leveraging in terms of  $CE^*$  are fairly modest in our setting, as the move from no leveraging in  $Z_8$  ( $m_{max} = 1$ ) to a considerable degree of leveraging in  $Z_9$  ( $m_{max} = 2$ ) only leads to a gain of less than 1%. A main reason for this is that the Merton fraction of our baseline agent is 0.25 so that, ideally, 25% of total wealth is invested in the risky asset. Thus leverage constraints on financial wealth will typically only be binding in a

<sup>8</sup>Note that we do not include a scenario without leverage constraints. At the beginning of the investment horizon, the demand for leveraging is so high that without a constraint we would see many scenarios with negative financial wealth at intermediate points in time. In combination with optimistic beliefs about human capital,  $\tilde{h}_1 > h_1$ , we would then see scenarios with a realized utility of negative infinity, implying an expected utility that is flat at negative infinity.

relatively short period early in the investment horizon, when total wealth is dominated by human capital. In Figure 9a we see that losses are limited when leverage positions are not allowed, as is the case in the “flexible pension scheme” proposed in the current Dutch reform where there is no intergenerational risk sharing via a solidarity buffer<sup>9</sup>. In particular, the constraint becomes binding when  $\tilde{\gamma}$  is small. Agents with a smaller  $\tilde{\gamma}$  wants to take higher risks due to underestimation of their own risk aversion. The leverage constraint keeps the agent from making this mistake, leading to a flat curve for small  $\tilde{\gamma}$  and, importantly, a lower bound on the possible losses from underestimation of one’s own risk aversion. By decreasing  $m_{max}$ , we increase the level of  $\tilde{\gamma}$  at which this effect kicks in. The price we pay for this lower bound is that it limits participants’ ability to borrow against their human capital when they are young. While the resulting welfare loss is small in the present example, it can be expected to be larger when the target investment fraction is higher, for example because true risk aversion  $\gamma$  is lower or expected returns  $\mu$  are higher.

Figure 9: Leverage



<sup>9</sup>In flexible contracts, there is the possibility of a so-called risk sharing buffer, however, its distribution rule cannot depend on realized returns.

## 4 Practical challenges

A major problem in the implementation of (collective) investment strategies based on risk preferences and risk capacities is to quantify and measure the two. In most of this paper, we looked at the outcomes that arise when there is a discrepancy between the true risk preferences and capacities and the risk preferences and capacities that form the basis of an investment strategy, trying to understand how sensitive the problem is to different types of discrepancies. Of course, this type of research should go hand in hand with attempts to measure and control the magnitudes of these discrepancies. Importantly, when we also account for statistical error in the assessment of market conditions, there are so many competing sources of uncertainty that a fully personalized, individually optimal investment solution clearly remains an illusion. This makes it even more important to aim at investment strategies that are robust to misspecifications.

When it comes to the measurement of risk capacities, there are practical dimensions to the problem that deserve attention. To come up with a fair assessment of risk capacity, both financial pension wealth and human capital need to be computed. These two numbers reflect the size of the pension pot so far and how much will still be contributed in the form of pension premiums. In an ideal setting, these computations would account for the full picture, including financial and housing wealth, the family situation, and different pension accounts. For instance, individuals can have pension accounts at different pension funds or insurance companies because they might have accrued pension rights with various jobs and employers, possibly even in different countries. Typically, this private information is not shared between pension providers (AFM, 2023).

On top of that, even with full information about the present situation, future income and thus contributions are uncertain. Many factors contribute here, including career stage, age, life events and the overall state of the economy. If there is a correlation between the stock market and salary, human capital is partly exposed to the same risks as financial wealth. Thus, in order to keep the risk exposure of total wealth constant, the risk exposure in financial wealth needs to be decreased if human capital is not risk-free. Finally, there are also non-market risks such as the risk of a health shock or a divorce, that add uncertainty to human capital in practice and can have a considerable impact as we discussed in the context of scenarios  $Z_4$  and  $Z_5$ . Relaxing the assumption of risk-free human capital is thus an interesting direction for further research.

Incorporating a state pension (such as the Dutch AOW) increases the human capital component of pension wealth, but leaves the financial capital unchanged.<sup>10</sup> Conse-

<sup>10</sup>In particular, the discounted sum of state pension payments can be collected in the terminal value  $H_T$  of the human capital process which then satisfies  $H_T > 0$ . One may debate whether “human capital” is the best name for this non-liquid part of pension wealth when the state pension is included.

quently, a higher risk exposure in financial wealth would be optimal. However, one can also argue that participants' true utility functions include a subsistence level, i.e., a positive minimal amount of wealth that is needed. This would lead to a HARA (i.e. shifted CRRA) rather than a standard CRRA utility function. If one then assumes that the subsistence level is equal to the level of the state pension, we return to a setting like our baseline model where the CRRA function is applied to the second pillar savings only. In this way, our results can be extended to cover the state pension in two different ways, either by including them in human capital or by assuming that they are equal to a subsistence level that is also included in preferences. A further investigation is beyond the scope of this paper.

## 5 Conclusion

Risk preferences, risk capacity, and financial market assumptions together determine the optimal investment decision. Mistakes in their assessment, estimation, or perception lead to suboptimal lifecycle investing. We investigate the impact that unanticipated changes have on the expected utility from pension wealth at retirement. If suboptimal lifecycles are implemented for some period of time – until the “moment of truth” at which it is realized what the true preferences and capacities are – there is a loss compared to what could have been achieved. We find that leverage constraints bound the loss due to underestimating the risk aversion. Alleviating this constraint can cause pension wealth to become negative – a feature that is not allowed within the new pension design. On the other hand, the loss due to overestimating risk aversion is also bounded since in the limit risk exposure is zero. The impact of wrong beliefs about future income seems to be even smaller compared to wrong beliefs about risk preferences, at least within most parameter ranges considered. Moreover, an overestimation of future income can counterbalance overestimation of the risk aversion because overestimation of future contributions leads to excessive investment in risky assets while overestimating the risk level leads to too little exposure, and vice versa. Of course, in the same way, different mistakes can also reinforce each other, for example when an overestimation of future income goes together with an underestimation of one’s risk aversion and an overly optimistic assessment of financial market conditions.

If a sizable drop in income is not foreseen, the impact can be substantial. Situations in which pension contributions disappear include disability or unemployment but also emigration or becoming self-employed. However, the latter two situations could entail that pension is accrued elsewhere. Factors like these should also be taken into account when assessing the risk capacity.

Interpreting our observations from another direction, we find that a perfect match between individual preferences and portfolio strategies, i.e., a full personalization, is not needed for close to optimal results. Instead, it seems key to look for strategies that are robust in the sense that they still work well under slightly different preferences and slightly different personal situations and market environments. Once we account for more sources of uncertainty besides the market itself, product features such as leverage constraints or built-in disability insurance may contribute much more to welfare than the illusion of a perfect match between the individually optimal investment fraction and the implemented one. Finally, a certain degree of aggregation across similar agents may help to avoid extreme choices that can sometimes arise as the result of extreme preferences or extreme personal circumstances – but also as the result of misperceptions or mistakes.



## References

- AFM (2023). Voorlopige leidraad risicopreferentieonderzoeken. *Autoriteit Financiële Markten*.
- Alserda, G. A., Dellaert, B. G., Swinkels, L., and van der Lecq, F. S. (2019). Individual pension risk preference elicitation and collective asset allocation with heterogeneity. *Journal of Banking & Finance*, 101:206–225.
- Balter, A., Schumacher, J. M., and Schweizer, N. (2022). Solving maxmin optimization problems via population games. *SSRN: 4264811*.
- Balter, A. G. and Schweizer, N. (2021). Robust decisions for heterogeneous agents via certainty equivalents. *arXiv preprint: 2106.13059*.
- Bodie, Z., Merton, R. C., and Samuelson, W. F. (1992). Labor supply flexibility and portfolio choice in a life cycle model. *Journal of Economic Dynamics and Control*, 16(3-4):427–449.
- Bokern, P., Linde, J., Riedl, A., Schmeets, H., and Werner, P. (2021). A survey of risk preference measures and their relation to field behavior. *Netspar Survey Paper*, 58.
- Bokern, P., Linde, J., Riedl, A., Schmeets, H., and Werner, P. (2022). Personal life events and individual risk preferences. *Netspar Design Paper*, 210.
- Campbell, J. Y., Cocco, J. F., Gomes, F. J., and Maenhout, P. J. (2001). Investing retirement wealth: A life-cycle model. In *Risk Aspects of Investment-Based Social Security Reform*, pages 439–482. University of Chicago Press.
- Cocco, J. F., Gomes, F. J., and Maenhout, P. J. (2005). Consumption and portfolio choice over the life cycle. *Review of Financial Studies*, 18(2):491–533.
- Conine, T. E., McDonald, M. B., and Tamarkin, M. (2017). Estimation of relative risk aversion across time. *Applied Economics*, 49(21):2117–2124.
- Joseph, A., Pelsser, A., and Werner, L. (2021). Beleggingsbeleid bij onzekerheid over risicobereidheid en budget. *Netspar Design Paper*, 174.
- Lever, M., Bonenkamp, J., and Cox, R. (2013). Eindrapportage ‘voor-en nadelen van de doorsneesystematiek’. *The Hague: CPB Policy Brief, Centraal Planbureau*.
- Nijman, T. (2022). De keuze tussen varianten uit het pensioenakkoord. *Netspar Board Brief*.
- Rogers, L. C. G. (2013). *Optimal Investment*. Springer.

## OVERZICHT UITGAVEN IN DE DESIGN PAPER SERIE

- 1 Naar een nieuw pensioencontract (2011)  
Lans Bovenberg en Casper van Ewijk
- 2 Langlevenrisico in collectieve pensioencontracten (2011)  
Anja De Waegenaere, Alexander Paulis en Job Stigter
- 3 Bouwstenen voor nieuwe pensioencontracten en uitdagingen voor het toezicht daarop (2011)  
Theo Nijman en Lans Bovenberg
- 4 European supervision of pension funds: purpose, scope and design (2011)  
Niels Kortleve, Wilfried Mulder and Antoon Pelsser
- 5 Regulating pensions: Why the European Union matters (2011)  
Ton van den Brink, Hans van Meerten and Sybe de Vries
- 6 The design of European supervision of pension funds (2012)  
Dirk Broeders, Niels Kortleve, Antoon Pelsser and Jan-Willem Wijckmans
- 7 Hoe gevoelig is de uittredeleeftijd voor veranderingen in het pensioenstelsel? (2012)  
Didier Fouarge, Andries de Grip en Raymond Montizaan
- 8 De inkomensverdeling en levensverwachting van ouderen (2012)  
MARIKE Knoef, Rob Alessie en Adriaan Kalwij
- 9 Marktconsistente waardering van zachte pensioenrechten (2012)  
Theo Nijman en Bas Werker
- 10 De RAM in het nieuwe pensioenakkoord (2012)  
Frank de Jong en Peter Schotman
- 11 The longevity risk of the Dutch Actuarial Association's projection model (2012)  
Frederik Peters, Wilma Nusselder and Johan Mackenbach
- 12 Het koppelen van pensioenleeftijd en pensioenaanspraken aan de levensverwachting (2012)  
Anja De Waegenaere, Bertrand Melenberg en Tim Boonen
- 13 Impliciete en expliciete leeftijdsdifferentiatie in pensioencontracten (2013)  
Roel Mehlkopf, Jan Bonenkamp, Casper van Ewijk, Harry ter Rele en Ed Westerhout
- 14 Hoofdlijnen Pensioenakkoord, juridisch begrepen (2013)  
Mark Heemskerk, Bas de Jong en René Maatman
- 15 Different people, different choices: The influence of visual stimuli in communication on pension choice (2013)  
Elisabeth Brügggen, Ingrid Rohde and Mijke van den Broeke
- 16 Herverdeling door pensioenregelingen (2013)  
Jan Bonenkamp, Wilma Nusselder, Johan Mackenbach, Frederik Peters en Harry ter Rele
- 17 Guarantees and habit formation in pension schemes: A critical analysis of the floor-leverage rule (2013)  
Frank de Jong and Yang Zhou
- 18 The holistic balance sheet as a building block in pension fund supervision (2013)  
Erwin Fransen, Niels Kortleve, Hans Schumacher, Hans Staring and Jan-Willem Wijckmans
- 19 Collective pension schemes and individual choice (2013)  
Jules van Binsbergen, Dirk Broeders, Myrthe de Jong and Ralph Koijen
- 20 Building a distribution builder: Design considerations for financial investment and pension decisions (2013)  
Bas Donkers, Carlos Lourenço, Daniel Goldstein and Benedict Dellaert

- 21 Escalerende garantietoezeggingen: een alternatief voor het StAr RAM-contract (2013)  
Servaas van Bilsen, Roger Laeven en Theo Nijman
- 22 A reporting standard for defined contribution pension plans (2013)  
Kees de Vaan, Daniele Fano, Herialt Mens and Giovanna Nicodano
- 23 Op naar actieve pensioenconsumenten: Inhoudelijke kenmerken en randvoorwaarden van effectieve pensioencommunicatie (2013)  
Niels Kortleve, Guido Verbaal en Charlotte Kuiper
- 24 Naar een nieuw deelnemergericht UPO (2013)  
Charlotte Kuiper, Arthur van Soest en Cees Dert
- 25 Measuring retirement savings adequacy; developing a multi-pillar approach in the Netherlands (2013)  
MARIKE KNOEF, Jim Been, Rob Alessie, Koen Caminada, Kees Goudswaard, and Adriaan Kalwij
- 26 Illiquiditeit voor pensioenfondsen en verzekeraars: Rendement versus risico (2014)  
Joost Driessen
- 27 De doorsneesystematiek in aanvullende pensioenregelingen: effecten, alternatieven en transitiepaden (2014)  
Jan Bonenkamp, Ryanne Cox en Marcel Lever
- 28 EIOPA: bevoegdheden en rechtsbescherming (2014)  
Ivor Witte
- 29 Een institutionele beleggersblik op de Nederlandse woningmarkt (2013)  
Dirk Brounen en Ronald Mahieu
- 30 Verzekeraar en het reële pensioencontract (2014)  
Jolanda van den Brink, Erik Lutjens en Ivor Witte
- 31 Pensioen, consumptiebehoeften en ouderenzorg (2014)  
MARIKE KNOEF, Arjen Hussem, Arjan Soede en Jochem de Bresser
- 32 Habit formation: implications for pension plans (2014)  
Frank de Jong and Yang Zhou
- 33 Het Algemeen pensioenfonds en de taakafbakening (2014)  
Ivor Witte
- 34 Intergenerational Risk Trading (2014)  
Jiajia Cui and Eduard Ponds
- 35 Beëindiging van de doorsneesystematiek: juridisch navigeren naar alternatieven (2015)  
Dick Boeijen, Mark Heemskerk en René Maatman
- 36 Purchasing an annuity: now or later? The role of interest rates (2015)  
Thijs Markwat, Roderick Molenaar and Juan Carlos Rodriguez
- 37 Entrepreneurs without wealth? An overview of their portfolio using different data sources for the Netherlands (2015)  
Mauro Mastrogiacomo, Yue Li and Rik Dillingh
- 38 The psychology and economics of reverse mortgage attitudes. Evidence from the Netherlands (2015)  
Rik Dillingh, Henriëtte Prast, Mariacristina Rossi and Cesira Urzì Brancati
- 39 Keuzevrijheid in de uittreedleeftijd (2015)  
Arthur van Soest
- 40 Afschaffing doorsneesystematiek: verkenning van varianten (2015)  
Jan Bonenkamp en Marcel Lever
- 41 Nederlandse pensioenopbouw in internationaal perspectief (2015)  
MARIKE KNOEF, Kees Goudswaard, Jim Been en Koen Caminada
- 42 Intergenerationele risicodeling in collectieve en individuele pensioencontracten (2015)  
Jan Bonenkamp, Peter Broer en Ed Westerhout
- 43 Inflation Experiences of Retirees (2015)  
Adriaan Kalwij, Rob Alessie, Jonathan Gardner and Ashik Anwar Ali
- 44 Financial fairness and conditional indexation (2015)  
Torsten Kleinow and Hans Schumacher
- 45 Lessons from the Swedish occupational pension system (2015)  
Lans Bovenberg, Ryanne Cox and Stefan Lundbergh

- 46 Heldere en harde pensioenrechten onder een PPR (2016)  
Mark Heemskerk, René Maatman en Bas Werker
- 47 Segmentation of pension plan participants: Identifying dimensions of heterogeneity (2016)  
Wiebke Eberhardt, Elisabeth Brüggem, Thomas Post and Chantal Hoet
- 48 How do people spend their time before and after retirement? (2016)  
Johannes Binswanger
- 49 Naar een nieuwe aanpak voor risicoprofiel-meting voor deelnemers in pensioenregelingen (2016)  
Benedict Dellaert, Bas Donkers, Marc Turlings, Tom Steenkamp en Ed Vermeulen
- 50 Individueel defined contribution in de uitkeringsfase (2016)  
Tom Steenkamp
- 51 Wat vinden en verwachten Nederlanders van het pensioen? (2016)  
Arthur van Soest
- 52 Do life expectancy projections need to account for the impact of smoking? (2016)  
Frederik Peters, Johan Mackenbach en Wilma Nusselder
- 53 Effecten van gelaagdheid in pensioen-documenten: een gebruikersstudie (2016)  
Louise Nell, Leo Lentz en Henk Pander Maat
- 54 Term Structures with Converging Forward Rates (2016)  
Michel Vellekoop and Jan de Kort
- 55 Participation and choice in funded pension plans (2016)  
Manuel García-Huitrón and Eduard Ponds
- 56 Interest rate models for pension and insurance regulation (2016)  
Dirk Broeders, Frank de Jong and Peter Schotman
- 57 An evaluation of the nFTK (2016)  
Lei Shu, Bertrand Melenberg and Hans Schumacher
- 58 Pensioenen en inkomensongelijkheid onder ouderen in Europa (2016)  
Koen Caminada, Kees Goudswaard, Jim Been en Marike Knoef
- 59 Towards a practical and scientifically sound tool for measuring time and risk preferences in pension savings decisions (2016)  
Jan Potters, Arno Riedl and Paul Smeets
- 60 Save more or retire later? Retirement planning heterogeneity and perceptions of savings adequacy and income constraints (2016)  
Ron van Schie, Benedict Dellaert and Bas Donkers
- 61 Uitstroom van oudere werknemers bij overheid en onderwijs. Selectie uit de poort (2016)  
Frank Cörvers en Janneke Wilschut
- 62 Pension risk preferences. A personalized elicitation method and its impact on asset allocation (2016)  
Gosse Alserda, Benedict Dellaert, Laurens Swinkels and Fieke van der Lecq
- 63 Market-consistent valuation of pension liabilities (2016)  
Antoon Pelsser, Ahmad Salahnejhad and Ramon van den Akker
- 64 Will we repay our debts before retirement? Or did we already, but nobody noticed? (2016)  
Mauro Mastrogiacomo
- 65 Effectieve ondersteuning van zelfmanagement voor de consument (2016)  
Peter Lapperre, Alwin Oerlemans en Benedict Dellaert
- 66 Risk sharing rules for longevity risk: impact and wealth transfers (2017)  
Anja De Waegenaere, Bertrand Melenberg and Thijs Markwat
- 67 Heterogeniteit in doorsneeproblematiek. Hoe pakt de transitie naar degressieve opbouw uit voor verschillende pensioenfondsen? (2017)  
Loes Frehen, Wouter van Wel, Casper van Ewijk, Johan Bonekamp, Joost van Valkengoed en Dick Boeijen
- 68 De toereikendheid van pensioenopbouw na de crisis en pensioenhervormingen (2017)  
Marike Knoef, Jim Been, Koen Caminada, Kees Goudswaard en Jason Rhuggenaath

- 69 De combinatie van betaald en onbetaald werk in de jaren voor pensioen (2017)  
Marleen Damman en Hanna van Solinge
- 70 Default life-cycles for retirement savings (2017)  
Anna Grebenchtchikova, Roderick Molenaar, Peter Schotman en Bas Werker
- 71 Welke keuzemogelijkheden zijn wenselijk vanuit het perspectief van de deelnemer? (2017)  
Casper van Ewijk, Roel Mehlkopf, Sara van den Bleeken en Chantal Hoet
- 72 Activating pension plan participants: investment and assurance frames (2017)  
Wiebke Eberhardt, Elisabeth Brüggem, Thomas Post en Chantal Hoet
- 73 Zerotopia – bounded and unbounded pension adventures (2017)  
Samuel Sender
- 74 Keuzemogelijkheden en maatwerk binnen pensioenregelingen (2017)  
Saskia Bakels, Agnes Joseph, Niels Kortleve en Theo Nijman
- 75 Polderen over het pensioenstelsel. Het debat tussen de sociale partners en de overheid over de ouderdagvoorzieningen in Nederland, 1945–2000 (2017)  
Paul Brusse
- 76 Van uitkeringsovereenkomst naar PPR (2017)  
Mark Heemskerk, Kees Kamminga, René Maatman en Bas Werker
- 77 Pensioenresultaat bij degressieve opbouw en progressieve premie (2017)  
Marcel Lever en Sander Muns
- 78 Bestedingsbehoeften bij een afnemende gezondheid na pensionering (2017)  
Lieke Kools en Marike Knoef
- 79 Model Risk in the Pricing of Reverse Mortgage Products (2017)  
Anja De Waegenaere, Bertrand Melenberg, Hans Schumacher, Lei Shu and Lieke Werner
- 80 Expected Shortfall voor toezicht op verzekeraars: is het relevant? (2017)  
Tim Boonen
- 81 The Effect of the Assumed Interest Rate and Smoothing on Variable Annuities (2017)  
Anne G. Balter and Bas J.M. Werker
- 82 Consumer acceptance of online pension investment advice (2017)  
Benedict Dellaert, Bas Donkers and Carlos Lourenço
- 83 Individualized life-cycle investing (2017)  
Gréta Oleár, Frank de Jong and Ingmar Minderhoud
- 84 The value and risk of intergenerational risk sharing (2017)  
Bas Werker
- 85 Pensioenwensen voor en na de crisis (2017)  
Jochem de Bresser, Marike Knoef en Lieke Kools
- 86 Welke vaste dalingen en welk beleggingsbeleid passen bij gewenste uitkeringsprofielen in verbeterde premieregelingen? (2017)  
Johan Bonekamp, Lans Bovenberg, Theo Nijman en Bas Werker
- 87 Inkomens- en vermogensafhankelijke eigen bijdragen in de langdurige ouderenzorg: een levensloopperspectief (2017)  
Arjen Hussem, Harry ter Rele en Bram Wouterse
- 88 Creating good choice environments – Insights from research and industry practice (2017)  
Elisabeth Brüggem, Thomas Post and Kimberley van der Heijden
- 89 Two decades of working beyond age 65 in the Netherlands. Health trends and changes in socio-economic and work factors to determine the feasibility of extending working lives beyond age 65 (2017)  
Dorly Deeg, Maaïke van der Noordt and Suzan van der Pas
- 90 Cardiovascular disease in older workers. How can workforce participation be maintained in light of changes over time in determinants of cardiovascular disease? (2017)  
Dorly Deeg, E. Burgers and Maaïke van der Noordt
- 91 Zicht op zzp-pensioen (2017)  
Wim Zwinkels, Marike Knoef, Jim Been, Koen Caminada en Kees Goudswaard
- 92 Return, risk, and the preferred mix of PAYG and funded pensions (2017)  
Marcel Lever, Thomas Michielsen and Sander Muns

- 93 Life events and participant engagement in pension plans (2017)  
Matthew Blakstad, Elisabeth Brügggen and Thomas Post
- 94 Parttime pensioneren en de arbeids-participatie (2017)  
Raymond Montizaan
- 95 Keuzevrijheid in pensioen: ons brein wil niet kiezen, maar wel gekozen hebben (2018)  
Walter Limpens en Joyce Vonken
- 96 Employability after age 65? Trends over 23 years in life expectancy in good and in poor physical and cognitive health of 65–74-year-olds in the Netherlands (2018)  
Dorly Deeg, Maaïke van der Noordt, Emiel Hoogendijk, Hannie Comijs and Martijn Huisman
- 97 Loslaten van de verplichte pensioenleeftijd en het organisatieklimaat rondom langer doorwerken (2018)  
Jaap Oude Mulders, Kène Henkens en Harry van Dalen
- 98 Overgangseffecten bij introductie degressieve opbouw (2018)  
Bas Werker
- 99 You're invited – RSVP! The role of tailoring in incentivising people to delve into their pension situation (2018)  
Milena Dinkova, Sanne Elling, Adriaan Kalwij en Leo Lentz
- 100 Geleidelijke uittreding en de rol van deeltijdpensioen (2018)  
Jonneke Bolhaar en Daniël van Vuuren
- 101 Naar een model voor pensioen-communicatie (2018)  
Leo Lentz, Louise Nell en Henk Pander Maat
- 102 Tien jaar UPO. Een terugblik en vooruitblik op inhoud, doelen en effectiviteit (2018)  
Sanne Elling en Leo Lentz
- 103 Health and household expenditures (2018)  
Raun van Ooijen, Jochem de Bresser en Marike Knoef
- 104 Keuzevrijheid in de uitkeringsfase: internationale ervaringen (2018)  
Marcel Lever, Eduard Ponds, Rik Dillingh en Ralph Stevens
- 105 The move towards riskier pension products in the world's best pension systems (2018)  
Anne G. Balter, Malene Kallestrup-Lamb and Jesper Rangvid
- 106 Life Cycle Option Value: The value of consumer flexibility in planning for retirement (2018)  
Sonja Wendel, Benedict Dellaert and Bas Donkers
- 107 Naar een duidelijk eigendomsbegrip (2018)  
Jop Tangelder
- 108 Effect van stijging AOW-leeftijd op arbeidsongeschiktheid (2018)  
Rik Dillingh, Jonneke Bolhaar, Marcel Lever, Harry ter Rele, Lisette Swart en Koen van der Ven
- 109 Is de toekomst gearriveerd? Data science en individuele keuzemogelijkheden in pensioen (2018)  
Wesley Kaufmann, Bastiaan Starink en Bas Werker
- 110 De woontevredenheid van ouderen in Nederland (2018)  
Jan Rouwendal
- 111 Towards better prediction of individual longevity (2018)  
Dorly Deeg, Jan Kardaun, Maaïke van der Noordt, Emiel Hoogendijk en Natasja van Schoor
- 112 Framing in pensioenkeuzes. Het effect van framing in de keuze voor beleggingsprofiel in DC-plannen naar aanleiding van de Wet verbeterde premieregeling (2018)  
Marijke van Putten, Rogier Potter van Loon, Marc Turlings en Eric van Dijk
- 113 Working life expectancy in good and poor self-perceived health among Dutch workers aged 55–65 years with a chronic disease over the period 1992–2016 (2019)  
Astrid de Wind, Maaïke van der Noordt, Dorly Deeg and Cécile Boot
- 114 Working conditions in post-retirement jobs: A European comparison (2019)  
Ellen Dingemans and Kène Henkens

- 115 Is additional indebtedness the way to increase mortgage–default insurance coverage? (2019)  
Yeorim Kim, Mauro Mastrogiacomio, Stefan Hochguertel and Hans Bloemen
- 116 Appreciated but complicated pension Choices? Insights from the Swedish Premium Pension System (2019)  
Monika Böhnke, Elisabeth Brügggen and Thomas Post
- 117 Towards integrated personal financial planning. Information barriers and design propositions (2019)  
Nitesh Bharosa and Marijn Janssen
- 118 The effect of tailoring pension information on navigation behavior (2019)  
Milena Dinkova, Sanne Elling, Adriaan Kalwij and Leo Lentz
- 119 Opleiding, levensverwachting en pensioenleeftijd: een vergelijking van Nederland met andere Europese landen (2019)  
Johan Mackenbach, José Rubio Valverde en Wilma Nusselder
- 120 Giving with a warm hand: Evidence on estate planning and bequests (2019)  
Eduard Suari–Andreu, Raun van Ooijen, Rob J.M. Alessie and Viola Angelini
- 121 Investeren in menselijk kapitaal: een gecombineerd werknemers– en werkgeversperspectief (2019)  
Raymond Montizaan, Merlin Nieste en Davey Poulissen
- 122 The rise in life expectancy – corresponding rise in subjective life expectancy? Changes over the period 1999–2016 (2019)  
Dorly Deeg, Maaïke van der Noordt, Noëlle Sant, Henrike Galenkamp, Fanny Janssen and Martijn Huisman
- 123 Pensioenaanvullingen uit het eigen woningbezit (2019)  
Dirk Brounen, Niels Kortleve en Eduard Ponds
- 124 Personal and work–related predictors of early exit from paid work among older workers with health limitations (2019)  
Nils Plomp, Sascha de Breij and Dorly Deeg
- 125 Het delen van langlevensrisico (2019)  
Anja De Waegenaere, Agnes Joseph, Pascal Janssen en Michel Vellekoop
- 126 Maatwerk in pensioencommunicatie (2019)  
S.K. Elling en L.R. Lentz
- 127 Dutch Employers’ Responses to an Aging Workforce: Evidence from Surveys, 2009–2017 (2019)  
Jaap Oude Mulders, Kène Henkens and Hendrik P. van Dalen
- 128 Preferences for solidarity and attitudes towards the Dutch pension system – Evidence from a representative sample (2019)  
Arno Riedl, Hans Schmeets and Peter Werner
- 129 Deeltijdpensioen geen wondermiddel voor langer doorwerken (2019)  
Henk–Wim de Boer, Tunga Kantarcı, Daniel van Vuuren en Ed Westerhout
- 130 Spaarmotieven en consumptiegedrag (2019)  
Johan Bonekamp en Arthur van Soest
- 131 Substitute services: a barrier to controlling long–term care expenditures (2019)  
Mark Kattenberg and Pieter Bakx
- 132 Voorstel keuzearchitectuur pensioensparen voor zelfstandigen (2019)  
Jona Linde
- 133 The impact of the virtual integration of assets on pension risk preferences of individuals (2019)  
Sesil Lim, Bas Donkers en Benedict Dellaert
- 134 Reforming the statutory retirement age: Policy preferences of employers (2019)  
Hendrik P. van Dalen, Kène Henkens and Jaap Oude Mulders
- 135 Compensatie bij afschaffing doorsnee–systematiek (2019)  
Dick Boeijen, Chantal de Groot, Mark Heemskerk, Niels Kortleve en René Maatman
- 136 Debt affordability after retirement, interest rate shocks and voluntary repayments (2019)  
Mauro Mastrogiacomio

- 137 Using social norms to activate pension plan members: insights from practice (2019)  
Joyce Augustus-Vonken, Pieter Verhallen, Lisa Brüggem and Thomas Post
- 138 Alternatieven voor de huidige verplichtstelling van bedrijfstakpensioenfondsen (2020)  
Erik Lutjens en Fieke van der Lecq
- 139 Eigen bijdrage aan ouderenzorg (2020)  
Pieter Bakx, Judith Bom, Marianne Tenand en Bram Wouterse
- 140 Inrichting fiscaal kader bij afschaffing doorsneesystematiek (2020)  
Bastiaan Starink en Michael Visser
- 141 Hervorming langdurige zorg: trends in het gebruik van verpleging en verzorging (2020)  
Pieter Bakx, Pilar Garcia-Gomez, Sara Rellstab, Erik Schut en Eddy van Doorslaer
- 142 Genetic health risks, insurance, and retirement (2020)  
Richard Karlsson Linnér and Philipp D. Koellinger
- 143 Publieke middelen voor particuliere ouderenzorg (2020)  
Arjen Hussem, Marianne Tenand en Pieter Bakx
- 144 Emotions and technology in pension service interactions: Taking stock and moving forward (2020)  
Wiebke Eberhardt, Alexander Henkel en Chantal Hoet
- 145 Opleidingsverschillen in levensverwachting: de bijdrage van acht risicofactoren (2020)  
Wilma J. Nusselder, José Rubio Valverde en Johan P. Mackenbach
- 146 Shades of Labor: Motives of Older Adults to Participate in Productive Activities (2020)  
Sonja Wendel and Benedict Dellaert
- 147 Raising pension awareness through letters and social media: Evidence from a randomized and a quasi-experiment (2020)  
Marika Knoef, Jim Been and Marijke van Putten
- 148 Infographics and Financial Decisions (2020)  
Ruben Cox and Peter de Goeij
- 149 To what extent can partial retirement ensure retirement income adequacy? (2020)  
Tunga Kantarcı and Jochem Zweerink
- 150 De steun voor een 'zwareberoepenregeling' ontleed (2020)  
Harry van Dalen, Kène Henkens en Jaap Oude Mulders
- 151 Verbeteren van de inzetbaarheid van oudere werknemers tot aan pensioen: literatuuroverzicht, inzichten uit de praktijk en de rol van pensioenuitvoerders (2020)  
Peter Lapperre, Henk Heek, Pascal Corten, Ad van Zonneveld, Robert Boulogne, Marieke Koeman en Benedict Dellaert
- 152 Betere risicospreiding van eigen bijdragen in de verpleeghuiszorg (2020)  
Bram Wouterse, Arjen Hussem en Rob Aalbers
- 153 Doorbeleggen met garanties? (2020)  
Roderick Molenaar, Peter Schotman, Peter Dekkers en Mark Irwin
- 154 Differences in retirement preferences between the self-employed and employees: Do job characteristics play an explanatory role? (2020)  
Marleen Damman, Dieuwke Zwier en Swenne G. van den Heuvel
- 155 Do financial incentives stimulate partially disabled persons to return to work? (2020)  
Tunga Kantarcı and Jan-Maarten van Sonsbeek
- 156 Wijzigen van de bedrijfstakpensioenregeling: tussen pensioenfondsbestuur en sociale partners (2020)  
J.R.C. Tangelder
- 157 Keuzes tijdens de pensioenopbouw: de effecten van nudging met volgorde en standaardopties (2020)  
Wilde Zijlstra, Jochem de Bresser en Marika Knoef
- 158 Keuzes rondom pensioen: implicaties op uitkeringssnelheid voor een heterogeen deelnemersbestand (2020)  
Servaas van Bilsen, Johan Bonekamp, en Eduard Ponds



- 159 Met big data inspelen op woonwensen en woongedrag van ouderen: praktische inzichten voor ontwerp en beleid (2020)  
Ioulia V. Ossokina en Theo A. Arentze
- 160 Economic consequences of widowhood: Evidence from a survivor's benefits reform in the Netherlands (2020)  
Jeroen van der Vaart, Rob Alessie and Raun van Ooijen
- 161 How will disabled workers respond to a higher retirement age? (2020)  
Tunga Kantarcı, Jim Been and Arthur van Soest
- 162 Deeltijdpensioenen: belangstelling en belemmeringen op de werkvloer (2020)  
Hanna van Solinge, Harry van Dalen en Kène Henkens
- 163 Investing for Retirement with an Explicit Benchmark (2020)  
Anne Balter, Lennard Beijering, Pascal Janssen, Frank de Jong, Agnes Joseph, Thijs Kamma and Antoon Pelsser
- 164 Vergrijzing en verzuim: impact op de verzekeringsvoorkeuren van werkgevers (2020)  
Remco Mallee en Raymond Montizaan
- 165 Arbeidsmarkteffecten van de pensioenpremiestystematiek (2020)  
Marieke Knoef, Sander Muns en Arthur van Soest
- 166 Risk Sharing within Pension Schemes (2020)  
Anne Balter, Frank de Jong en Antoon Pelsser
- 167 Supporting pension participants: Three lessons learned from the medical domain for better pension decisions (2021)  
Jelle Strikwerda, Bregje Holleman and Hans Hoeken
- 168 Variable annuities with financial risk and longevity risk in the decumulation phase of Dutch DC products (2021)  
Bart Dees, Frank de Jong and Theo Nijman
- 169 Verloren levensjaren als gevolg van sterfte aan Covid-19 (2021)  
Bram Wouterse, Frederique Ram en Pieter van Baal
- 170 Which work conditions can encourage older workers to work overtime? (2021)  
Raymond Montizaan and Annemarie Kuenn-Nelen
- 171 Herverdeling van individueel pensioenvermogen naar partnerpensioen: een stated preference-analyse (2021)  
Raymond Montizaan
- 172 Risicogedrag na een ramp; implicaties voor pensioenen (2021)  
Martijn de Vries
- 173 The Impact of Climate Change on Optimal Asset Allocation for Long-Term Investors (2021)  
Mathijs Cosemans, Xander Hut and Mathijs van Dijk
- 174 Beleggingsbeleid bij onzekerheid over risicobereidheid en budget (2021)  
Agnes Joseph, Antoon Pelsser en Lieke Werner
- 175 On the Resilience of ESG Stocks during COVID-19: Global Evidence (2021)  
Gianfranco Gianfrate, Tim Kievid & Mathijs van Dijk
- 176 De solidariteitsreserve juridisch ontrafeld (2021)  
Erik Lutjens en Herman Kappelle
- 177 Hoe vertrouwen in politiek en maatschappij doorwerkt in vertrouwen in pensioeninstellingen (2021)  
Harry van Dalen en Kène Henkens
- 178 Gelijke rechten, maar geen gelijke pensioenen: de gender gap in Nederlandse tweedepijlerpensioenen (2021)  
Suzanne Kali, Jim Been, Marieke Knoef en Albert van Marwijk Kooy
- 179 Completing Dutch pension reform (2021)  
Ed Westerhout, Eduard Ponds and Peter Zwaneveld
- 180 When and why do employers hire and rehire employees beyond normal retirement age? (2021)  
Orlaith C. Tunney and Jaap Oude Mulders
- 181 Family and government insurance: Wage, earnings, and income risks in the Netherlands and the U.S. (2021)  
Mariacristina De Nardi, Giulio Fella, Marieke Knoef, Gonzalo Paz-Pardo and Raun van Ooijen

- 182 Het gebruik van data in de pensioenmarkt (2021)  
Willem van der Deijl, Marije Kloek, Koen Vaassen en Bas Werker
- 183 Applied Data Science in the Pension Industry: A Survey and Outlook (2021)  
Onaopepo Adekunle, Michel Dumontier and Arno Riedl
- 184 Individual differences in accessing personalized online pension information: Inertia and a digital hurdle (2021)  
Milena Dinkova, Adriaan Kalwij & Leo Lentz
- 185 Transitie: gevoeligheid voor veronderstellingen en omstandigheden (2021)  
Anne Balter, Jan Bonenkamp en Bas Werker
- 186 De voordelen van de solidariteitsreserve ontrafeld (2021)  
Servaas van Bilsen, Roel Mehlkopf en Antoon Pelsser
- 187 Consumption and time use responses to unemployment (2021)  
Jim Been, Eduard Suari-Andreu, Marike Knoef en Rob Alessie
- 188 Wat is inertie? (2021)  
Marijke van Putten en Robert-Jan Bastiaan de Rooij
- 189 The effect of the Dutch financial assessment framework on the mortgage investments of pension funds (2021)  
Yeorim Kim and Mauro Mastrogiacomo
- 190 The Recovery Potential for Underfunded Pension Plans (2021)  
Li Yang, Antoon Pelsser and Michel Vellekoop
- 191 Trends in verschillende gezondheidsindicatoren: de rol van opleidingsniveau (2021)  
Wilma J. Nusselder, José Rubio Valverde en Dorly Deeg
- 192 Toedeling van rendementen met spreiding (2021)  
Anne Balter en Bas Werker
- 193 Occupational pensions, macroprudential limits, and the financial position of the self-employed (2021)  
Francesco G. Caloia, Stefan Hochguertel and Mauro Mastrogiacomo
- 194 How do spouses respond when disability benefits are lost? (2021)  
Mario Bernasconi, Tunga Kantarci, Arthur van Soest, and Jan-Maarten van Sonsbeek
- 195 Pension Payout Preferences (2021)  
Rik Dillingh and Maria Zumbuehl
- 196 Naar de kern van pensioenkeuzes (2021)  
Jelle Strikwerda, Bregje Holleman en Hans Hoeken
- 197 The Demand for Retirement Products: The Role of Withdrawal Flexibility and Administrative Burden (2021)  
Pim Koopmans, Marike Knoef and Max van Lent
- 198 Stapelen van keuzes; interacties in keuze-architectuur en tussen tijd en risico (2021)  
Jona Linde en Ingrid Rohde
- 199 Arbeidsmarktstatus tussen de 65ste verjaardag en de AOW-leeftijd: verschillen tussen opleidingsgroepen (2021)  
Wilma J. Nusselder, Marti K. Rado en Dorly J.H. Deeg
- 200 Geheugenloos spreiden met gelijke aanpassingen (2021)  
Sander Muns
- 201 Bevoegdheidsverdeling sociale partners en pensioenfondsen bij stelseltransitie (2022)  
René Maatman en Mark Heemskerk
- 202 Matchmaking in pensioenland: welk pensioen past bij welke deelnemer? (2022)  
Marike Knoef, Rogier Potter van Loon, Marc Turlings, Marco van Toorn, Floske Weehuizen, Bart Dees en Jorgo Goossens
- 203 Inkomenseffecten bij en na invaren in het nieuwe pensioencontract (2022)  
Sander Muns, Theo Nijman en Bas Werker
- 204 Pensioenvoorbereiding van zzp'ers tijdens de coronacrisis (2022)  
Marleen Damman en Gerbert Kraaykamp
- 205 Een reële oriëntatie van het nieuwe pensioencontract (2022)  
Rens van Gastel, Niels Kortleve, Theo Nijman en Peter Schotman
- 206 Infographics and financial decisions: an eye-tracking experiment (2022)  
Hong Phuoc (Michael) Vo, Reinier Cozijn and Peter de Goeij

- 207 Eliciting Pension Beneficiaries' Sustainability Preferences (2022)  
Rob Bauer, Tobias Ruof and Paul Smeets
- 208 No pension and no house? The effect of LTV limits on the housing wealth accumulation of the self-employed (2022)  
Mauro Mastrogiacomo and Cindy Biesenbeek
- 209 Drawing Up the Bill: Does Sustainable Investing Affect Stock Returns Around the World? (2022)  
Rómulo Alves, Philipp Krueger and Mathijs van Dijk
- 210 Personal life events and individual risk preferences  
Paul Bokern, Jona Linde, Arno Riedl, Hans Schmeets and Peter Werner
- 211 Trust and Distrust in Pension Providers in Times of Decline and Reform. Analysis of Survey Data 2004–2021  
Harry van Dalen and Kène Henkens
- 212 Diversiteit en inclusie in pensioenfondsbesturen (2022)  
Tanachia Ashikali and Floortje Fontein
- 213 NDC-pensioen: bruikbaar alternatief voor Nederland? Verkenning van routes voor versterking pensioen voor allen (2022)  
Casper van Ewijk, Lex Meijdam en Eduard Ponds
- 214 Visuele communicatie van onzekere pensioenuitkeringen (2022)  
Lisanne van Weelden, Maaïke Jongenelen, Marloes van Moort en Hans Hoeken
- 215 Uitkeringseffecten en kostendekkende premies in het nieuwe nabestaandenpensioen (2022)  
Sander Muns, Theo Nijman en Bas Werker
- 216 A comparison of pension-relevant preferences, traits, skills, and attitudes between the self-employed and employees in the Netherlands (2022)  
Paul Bokern, Jona Linde, Arno Riedl, Hans Schmeets and Peter Werner
- 217 Het pensioenperspectief van basisbanen (2022)  
Ton Wilthagen, Zeger Kluit en Michael Visser
- 218 Carbon Bias in Index Investing (2022)  
Mathijs Cosemans and Dirk Schoenmaker
- 219 Measuring Risk Capacity (2022)  
Rob Alessie, Viola Angelini and Lars Kleinhuis
- 220 Participatiehypotheken als impuls voor mobiliseren woningkapitaal: een interessante optie voor pensioenfondsen (2023)  
Casper van Ewijk, Arjen Gielen, Marike Knoef, Mauro Mastrogiacomo en Alfred Slager
- 221 Trust in Pension Funds, Or the Importance of Being Financially Sound (2023)  
Hendrik P. van Dalen and Kène Henkens
- 222 De pensioenvoorziening in Nederland, Duitsland, het Verenigd Koninkrijk en Zwitserland: een rechtsvergelijkend onderzoek (2023)  
Jessica van den Heuvel-Warren
- 223 Sustainable Development Goals and Sovereign Bond Spreads: Investor Implications (2023)  
Eline ten Bosch, Mathijs van Dijk, and Dirk Schoenmaker
- 224 Show Me My Future: Data-Driven Storytelling and Pension Communication (2023)  
Kay Schroeder, Inka Eberhardt, Wiebke Eberhardt and Alexander Henkel
- 225 Shocks to Occupational Pensions and Household Savings (2023)  
Francesco Caloia, Mauro Mastrogiacomo and Irene Simonetti
- 226 Vertrouwen in partijen in het Nederlandse pensioenveld: een kwalitatief onderzoek onder deelnemers, consultants en adviseurs (2023)  
Jelle Strikwerda, Bregje Holleman en Hans Hoeken
- 227 Trust in the financial performance of pension funds, public perception, and its effect on participation in voluntary pension saving plans (2023)  
Floor Goedkoop, Madi Mangan, Mauro Mastrogiacomo and Stefan Hochguertel

- 228 Measuring sustainability preferences of pension members – A methodological proposition and a case study of a UK pension fund (2023)  
Rob Bauer, Marco Ceccarelli, Katrin Gödker, and Paul Smeets
- 229 Invaren of niet invaren door pensioenfondsen: economische en juridische aspecten (2023)  
Casper van Ewijk en Mark Heemskerk
- 230 Stated product choices of heterogeneous agents are largely consistent with standard models (2023)  
Bart Dees, Theo Nijman and Arthur van Soest
- 231 What comes to mind when considering looking into and/or adjusting one's pension? An empirical study among UK and US residents (2023)  
Eric van Dijk, Marcel Zeelenberg, Wändi Bruine de Bruin and Robert-Jan Bastiaan de Rooij
- 232 Taakafbakening: houdbaarheid in toekomstig pensioenstelsel (2023)  
Erik Lutjens en Hans van Meerten
- 233 A comparison of risk preference elicitation methods and presentation formats (2023)  
Jorgo Goossens, Marike Knoef, Bart Kuijpers, Rogier Potter van Loon, Eduard Ponds, Arno Riedl, Siert Vos
- 234 The Effects of Online Financial Endorsements on the Investment Behavior of Young Retail Investors (2023)  
Peter de Goeij and Emre Kaan
- 235 Communicatie over de toedeling van vermogen – of het antwoord op de vraag: Ga ik erop voor- of achteruit? (2023)  
Lisa Brügger, Annemarie van Hekken en Bas Werker
- 236 Challenges of Automated Financial Advice: Definition and Ethical Considerations (2023)  
Robert Gianni, Minou van der Werf, Lisa Brügger, Darian Meacham, Jens Hogreve, Thomas Post and Jonas Heller
- 237 The impact of uncertainty in risk preferences and risk capacities on lifecycle investment (2023)  
Anne G. Balter, Rob van den Goorbergh en Nikolaus Schweizer



Network for Studies on Pensions, Aging and Retirement

This is a publication of:  
Netspar  
Phone +31 13 466 2109  
E-mail [info@netspar.nl](mailto:info@netspar.nl)  
[www.netspar.nl](http://www.netspar.nl)

November 2023